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Multiple Scattering Corrections for the Associated-Particle Neutron Time-of-Flight Technique

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Multiple Scattering Corrections for the Associated-Particle Neutron Time-of-Flight Technique

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Abstract

The computer code, MAGGIE, for the calculation of multiple scattering and sample attenuation in neutron differential cross-section measurements, has been revised and corrected. The particular case of the scattering geometry required by the associated-particle time-of-flight is considered in detail.

Key words: associated-particle, cross-section, Monte Carlo, multiple scattering, neutron, time-of-flight

MULTIPLE SCATTERING CORRECTIONS FOR THE ASSOCIATED-PARTICLE
NEUTRON TIME-OF-FLIGHT TECHNIQUE

Allan C. B. Richardson

I. INTRODUCTION

Measurements of fast neutron elastic and inelastic differential cross sections have, for many years now, usually been done using one of two time-of-flight techniques. The first of these requires a pulsed source of neutrons, and energy separation of the various neutron groups is then achieved by time correlation of the scattered neutrons with the incident neutron pulse. This technique has the advantage of flexibility of incident neutron energy and intensity, and the disadvantages of a relatively high time-correlated background and a low duty cycle. The other, and less commonly used, technique utilizes the detection of a charged particle from the neutron source reaction to tag the incident neutrons in time and direction. Energy separation of the various scattered neutron groups is then achieved by time correlation with the incident neutrons. This "associated-particle technique" has the advantages of very small time-correlated background, inherent absolute determination of the incident correlated neutron flux, and high duty cycle; but it suffers from limitations on the available neutron intensity and energy. However, at energies and intensities where this technique is applicable, it is the method of choice, since it is capable of yielding results of high accuracy without the ambiguities introduced by the time-correlated backgrounds and the massive shielding required by pulsed source techniques. The source reactions eligible for this method are those involving very light nuclei, and therefore capable of producing a light (and thus energetic) stable recoil nucleus. The $T(d,n)^4\text{He}$ reaction, producing 14-15 MeV neutrons at 90° over a rather wide range of incident particle energies, is most commonly used; other reactions that have been employed are $D(d,n)^3\text{He}$ and $T(p,n)^3\text{He}$, both of which produce lower energy neutrons. We will confine the discussion here to the $T(d,n)^4\text{He}$ case, although the method described is more generally applicable.

The associated-particle technique has scattering sample requirements that are quite different from those for a pulsed source. Instead of a relatively uniform incident neutron flux across the sample, the correlated neutron beam is highly directional. The angular distribution about the neutron beam line is usually well approximated by

$$I = I_0 e^{-\left(\frac{\theta}{\theta_0}\right)^2},$$

with θ_0 typically only a few degrees [1]. This property can be very useful [2]. It provides a high degree of neutron collimation without the need for massive collimators, which, in the case of 14 MeV neutrons, can produce substantial degradation of the initially monoenergetic neutron

beam. However, it forces the use of scattering samples of uniform thickness so that the cylindrical or spherical samples commonly used to simplify multiple scattering corrections are immediately ruled out. Otherwise a detailed knowledge of the neutron beam shape and extremely accurate alignment of this beam with respect to the scattering sample is needed. This alignment problem is further complicated because the center of the neutron beam slowly moves back as the neutron producing target ages with use. In measuring angular distributions of scattered neutrons it is of course also desirable to reduce the amount of scattering sample not directly in the neutron beam, so as to minimize multiple scattering.

A scattering sample in the form of a truncated cone, axis lying along the neutron beam, best satisfies all of these requirements. The origin of this cone is taken sufficiently far behind the source to allow for finite spot size on the neutron producing target, to provide some flexibility in alignment, and also to make allowance for changes due to target aging during a run. In order to make best use of the available neutron intensity, one must also use the thickest sample possible. The limit is set by either the angular resolution required at 90° or the time resolution required. A typical geometry is shown in figure 1.

In either case the resulting samples are sufficiently thick to require a careful multiple scattering correction. None of the analytical techniques [3], useful at energies up to a few MeV, are adequate at 14 MeV, the energy most commonly used for measurements of this type, since at energies above 6-7 MeV the diffraction peaks in the elastic angular distributions become too numerous. The only method of sufficient generality is the Monte Carlo technique. A survey of existing Monte Carlo codes revealed none for this particular geometry, but it was immediately apparent that the code "MAGGIE," developed by Parker, Towle, Sams, et al. at Aldermaston [4,5] contained all of the other elements important to such a calculation. For example, this code easily accommodates the neutron source distribution specified above. In addition, MAGGIE calculates an energy spectrum at each angle, so that false peaks due to double scattering can easily be identified. This sophistication is often useful, for example: the measurement of inelastic scattering from the very weakly excited $7.66 \text{ MeV } 0^+$ level in ^{12}C is easily confused by double scattering from the more easily excited $4.43 \text{ MeV } 2^+$ level in this nucleus.

A corollary need of any Monte Carlo neutronic calculation is an easily accessible, but at the same time sufficiently general, file program for the nuclear data required. This was available in a companion code to MAGGIE, entitled MOULD [6]. We have therefore modified the code MAGGIE so that it now handles the geometry required for associated-particle time-of-flight measurements. During the course of this modification we also corrected a few coding errors found in the original version, and made several additional modifications, principally updating the code to current computer syntax and capabilities.

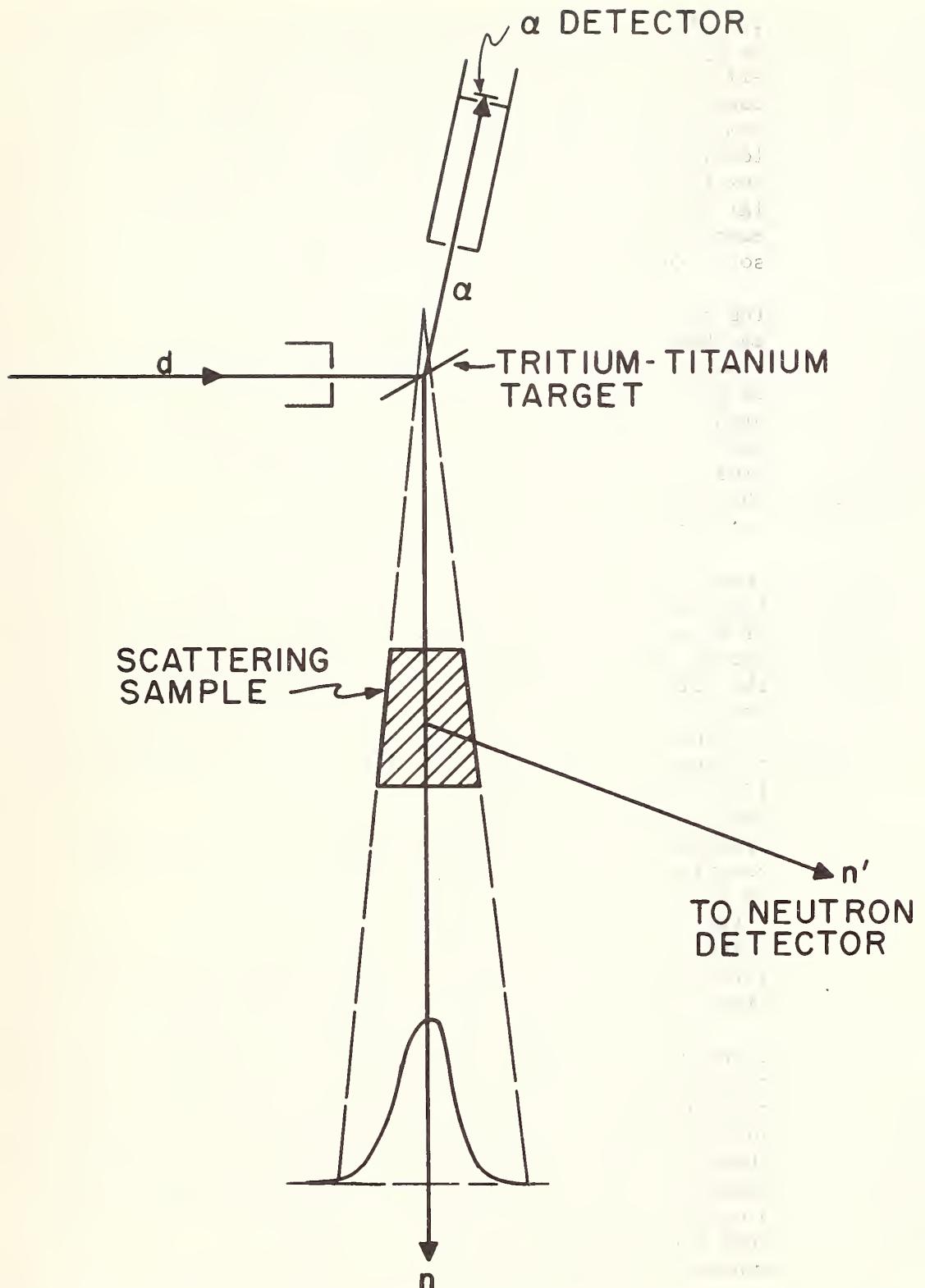


Fig. 1. The experimental geometry for associated-particle measurements at 14 MeV. The associated neutron intensity profile is indicated at the bottom of the figure.

Although a complete description of the code would be out of place here (see references 4 and 5 for details), a general overview of the program will facilitate later discussion of specific details. The point of view adopted is first to sample the scattering sample geometry and the available nuclear interactions using straightforward Monte Carlo techniques. Then, at each collision point, the weighted probability of scattering and escape to each of 33 detector positions (angles) in a half-plane lying to one side of the neutron beam axis is computed using the experimental data for elastic events and each of those inelastic processes of interest. The use of weighted probabilities of scattering to each of the detector positions at the final collision in the sample in place of a completely Monte Carlo approach results in a greatly reduced computation time. This is because the small solid angle subtended by each of the detectors (typically 10^{-3}) makes a final Monte Carlo scattering particularly inefficient. The output angular distributions obtained from applying this procedure to, typically, 1000 interacting neutrons are then reflected about the experimental input data and used as input for a second iteration. Two or three iterations are usually sufficient to obtain a convergent result.

In section II we give a description of the changes made in the code. First, the new coding for the scattering geometry used in the associated particle technique is described. Next we discuss a number of coding errors in the original version. Finally some changes are described that simplify the code and adopt it to FORTRAN V syntax. In section III we give some results obtained using data from the scattering of 14 MeV neutrons on natural carbon. A listing of those subroutines entirely rewritten or having extensive changes is given in Appendix A. In figure 2 the calling sequence for all of the components of the program is shown. A brief description of all of these subroutines appears in Appendix B.

II. DESCRIPTION OF MODIFICATIONS TO THE MONTE CARLO CODE MAGGIE

A. Changes Due to the New Scattering Sample Shape

Four subroutines are affected by changing the shape of the scattering sample. These are: 1) subroutine INPUT - those sections where scatterer parameters are read in and the flux attenuation factor is calculated are affected. The flux attenuation factor is defined as the ratio of incident flux along the axis of the sample to average flux in the entire sample. 2) CRNEU, the subroutine that creates incident neutrons at the entrance face of the scatterer by random sampling of the incident neutron spatial distribution. 3) TRACK, the tracking subroutine. 4) FPATH, the subroutine for calculating the probability of neutron escape from the sample in the direction of each of the assumed detector positions, for each collision point arrived at in TRACK.

It is worth noting here, although not necessary to what follows, that the data used for a) the neutron track lengths in the Monte Carlo sampling of the sample shape from subroutine EGMV, and b) the Monte Carlo sampling of reaction type and angular distribution at each collision by subroutine

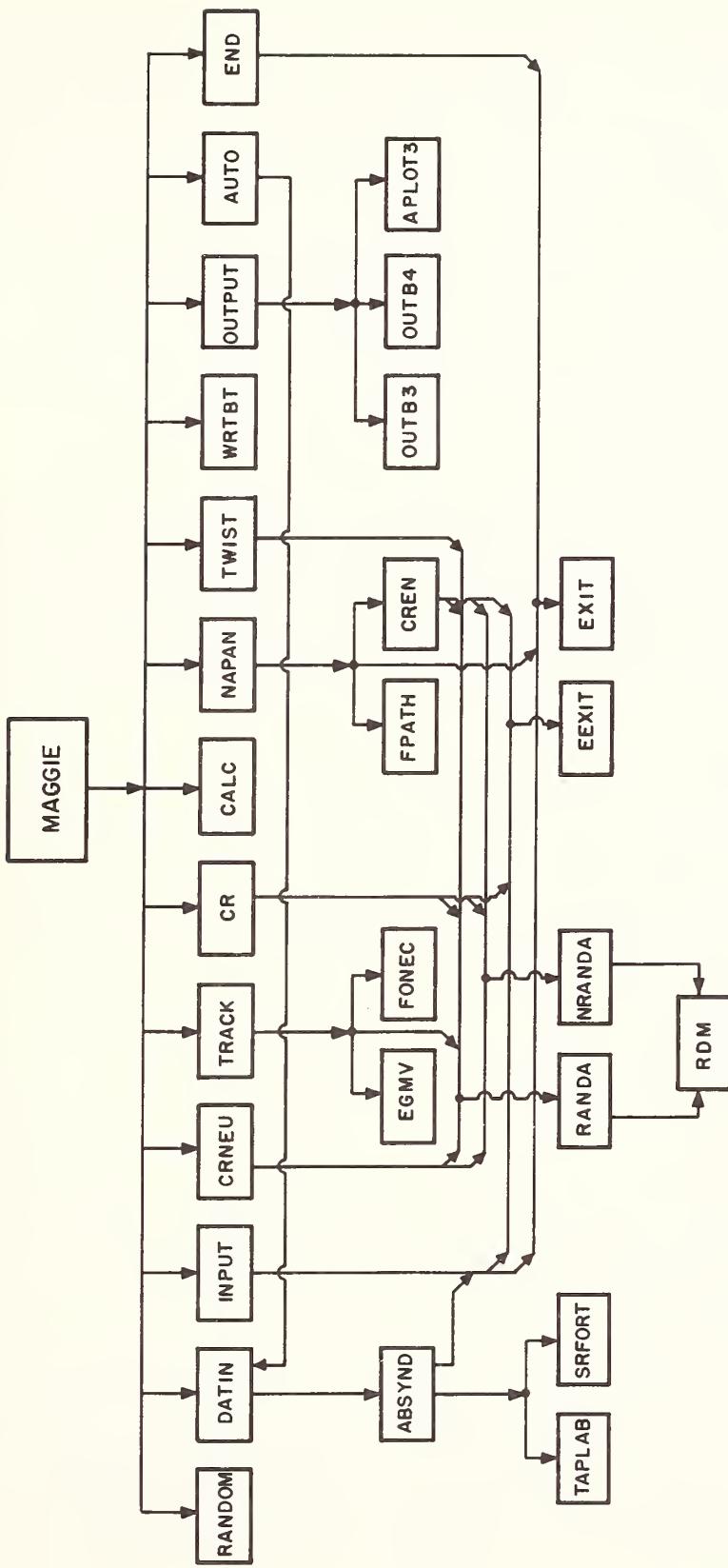


Fig. 2. The calling hierarchy for the present version of code MAGGIE.

CR, as well as c) the transmission probabilities in the direction of the detectors used in subroutines FPATH and NAPAN, are all drawn from the MOULD nuclear data file tape and not from input experimental data. The only experimental data employed are angular distributions used for the calculation of the scores for the relative probability of scattering to the various assumed detector positions in subroutine NAPAN. The elastic angular distribution (for the incident neutron energy only) used here is also automatically updated after each iteration by the subroutine AUTO. Thus it may be necessary to update the angular distributions on the MOULD file tape before and during the course of data-processing.

We now describe the changes due to the new scattering geometry in some detail for each of the subroutines affected.

1. INPUT

a. Cards 0207-0226 are changed to eliminate parameters required for samples consisting of concentric cylindrical shells, with common axes perpendicular to the beam axis, and to substitute those needed to characterize a truncated cone sample, axis lying along the neutron beam, and origin behind the neutron source. The new variables are HITE, FRAD, and ANGLE; the height, entrance face radius, and half-angle of the sample, respectively. HITE is immediately redefined as HITE/2, a more convenient quantity in subsequent calculations.

b. Card 0245, the calculation of the maximum angle subtended by the scattering sample at the neutron source, is changed to conform to the new geometry.

c. Cards 0301-0303 have been replaced. The correct expression for the flux attenuation factor for the new geometry is

$$\frac{F_o}{F} = \frac{K(o)}{\bar{K}} \cdot \frac{C}{N\lambda} \cdot \frac{h(r_1^2 + r_1 \Delta r + \Delta r^2/3)}{(1 - \cos \theta_m) d^2},$$

where h is the half-length of the scattering sample, r_1 the radius of its entrance face, Δr the difference in radii of the entrance and exit faces, and d the distance from the source to the entrance face of the sample. The remaining symbols are defined as in the original.

d. The original version of MAGGIE utilized a sample which was not symmetric about the axis of the incident neutron flux. Thus the experimental sampling of scattered neutrons in the detector plane was not truly representative of the scattering into 4π , which is employed in the program to calculate the flux attenuation factors and which are used in turn to infer the integrated cross-sections. This necessitated a small correction which was calculated with the help of a classification of the outgoing

Monte Carlo tracks vs. energy and the angle with respect to the scattering sample axis. Since the present scattering sample is symmetric about the incident neutron flux the experimental sampling of scattered neutrons in the detector plane is representative, and no correction is required. Accordingly, cards 0331-0338 in INPUT, cards 1544-1548 in DATIN, and cards 1735-1743 in MAGGIE are deleted. Card 1734 of MAGGIE is replaced by the statement

20 CONTINUE

The output of this table, by cards 3695-3715 of subroutine OUTB3, is also deleted.

2. CRNEU

Cards 3117-3119, 3140-3141, 3143-3147 and 3151 are replaced as shown in the listing. The new coding creates neutrons randomly scattered over the face of the conical scattering sample, in accordance with the specified spatial distribution. The old reference to multiple materials is not deleted, but the sample is now designated "material one." Similarly, the register containing neutrons which miss the sample is retained, although for this geometry misses occur with very low frequency.

3. TRACK

The entire subroutine has been replaced. The geometry is illustrated in figure 3. The subroutine is entered with the starting point (x_0, y_0, z_0) and the direction cosines $(\cos\theta_x, \cos\theta_y, \cos\theta_z)$ already defined. A random sampling of the neutron mean free path establishes the track length to the next possible collision. The track vector is then extended until it intersects the plane determined by the endface of the sample in the direction of travel of the neutron, and the path length from the starting point to this intersection is computed. A comparison of this intersection point with the radius of the endface establishes whether the track is in the direction of the endface or the curved surface of the sample, and the program branches accordingly. If the track passes through the endface, the path length calculated above is compared with the Monte Carlo track length to the next collision and the coordinates of collision or escape from the surface of the sample as well as the time elapsed along the track are computed in a straight-forward way.

We consider now the procedure used for a neutron headed toward a curved surface of the scattering sample. The coordinates of the endpoint of the previously determined Monte Carlo track length are first found. These are used to calculate the projected distance, perpendicular to the symmetry axis, of this endpoint from the symmetry axis, as well as the length of the radius of the sample lying along this projection. Comparison of these quantities determines whether a collision occurs within the sample or not. If so, the coordinates are already known and the time elapsed along the track is all that remains to be calculated. If not, it is necessary to calculate the coordinates of the neutron's exit from

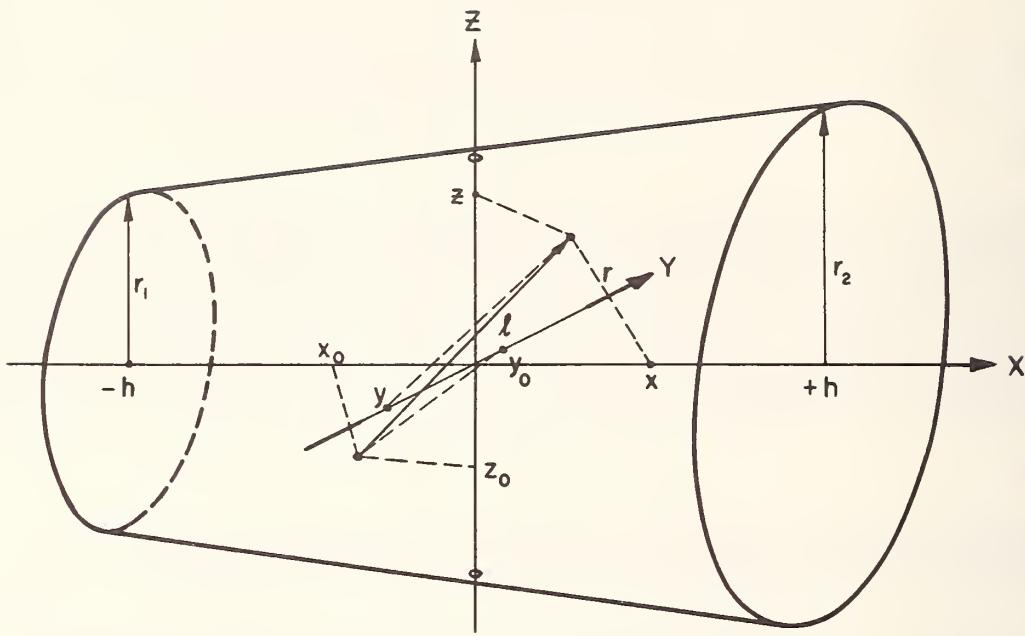


Fig. 3. The geometry for subroutine TRACK. The trajectory shown is that of a neutron which, after collision at point x_0 , y_0 , z_0 escapes from the curved surface of the sample at point x , y , z .

the surface of the cone. Designate ℓ the path length to the surface and x, y, z the coordinates of the intersection of the track with the surface. We have, referring to figure 3,

$$x - x_o = \ell \cos \theta_x$$

$$y - y_o = \ell \cos \theta_y$$

$$z - z_o = \ell \cos \theta_z ,$$

so that the projected distance, r , from the symmetry axis of the cone to the point (x, y, z) is given by

$$\begin{aligned} r^2 &= y^2 + z^2 \\ &= \ell^2 \sin^2 \theta_x + 2\ell(y_o \cos \theta_y + z_o \cos \theta_z) + y_o^2 + z_o^2 , \end{aligned} \quad (1)$$

where we have used the identity

$$\cos^2 \theta_x + \cos^2 \theta_y + \cos^2 \theta_z = 1 .$$

Since we know the parameters of the cone we can also calculate r from the x coordinate (again see figure 3.):

$$r = r_1 + (h+x) \tan \theta_o , \quad (2)$$

where θ_o is the half-angle of the cone. Eliminating r from eqⁿs. (1) and (2) and arranging the terms as a quadratic in ℓ , we obtain

$$\begin{aligned} &\ell^2 \left[1 - \cos^2 \theta_x (1 + \tan^2 \theta_o) \right] \\ &+ 2\ell \left[y_o \cos \theta_y + z_o \cos \theta_z - \cos \theta_x (r_1 \tan \theta_o + h + x_o) \tan^2 \theta_o \right] \\ &+ \left[y_o^2 + z_o^2 - (r_1 + (h+x_o) \tan \theta_o)^2 \right] = 0 . \end{aligned} \quad (3)$$

The positive root of this equation is the required path length to the surface, and the subroutine FONEC is then called to provide the x, y , and

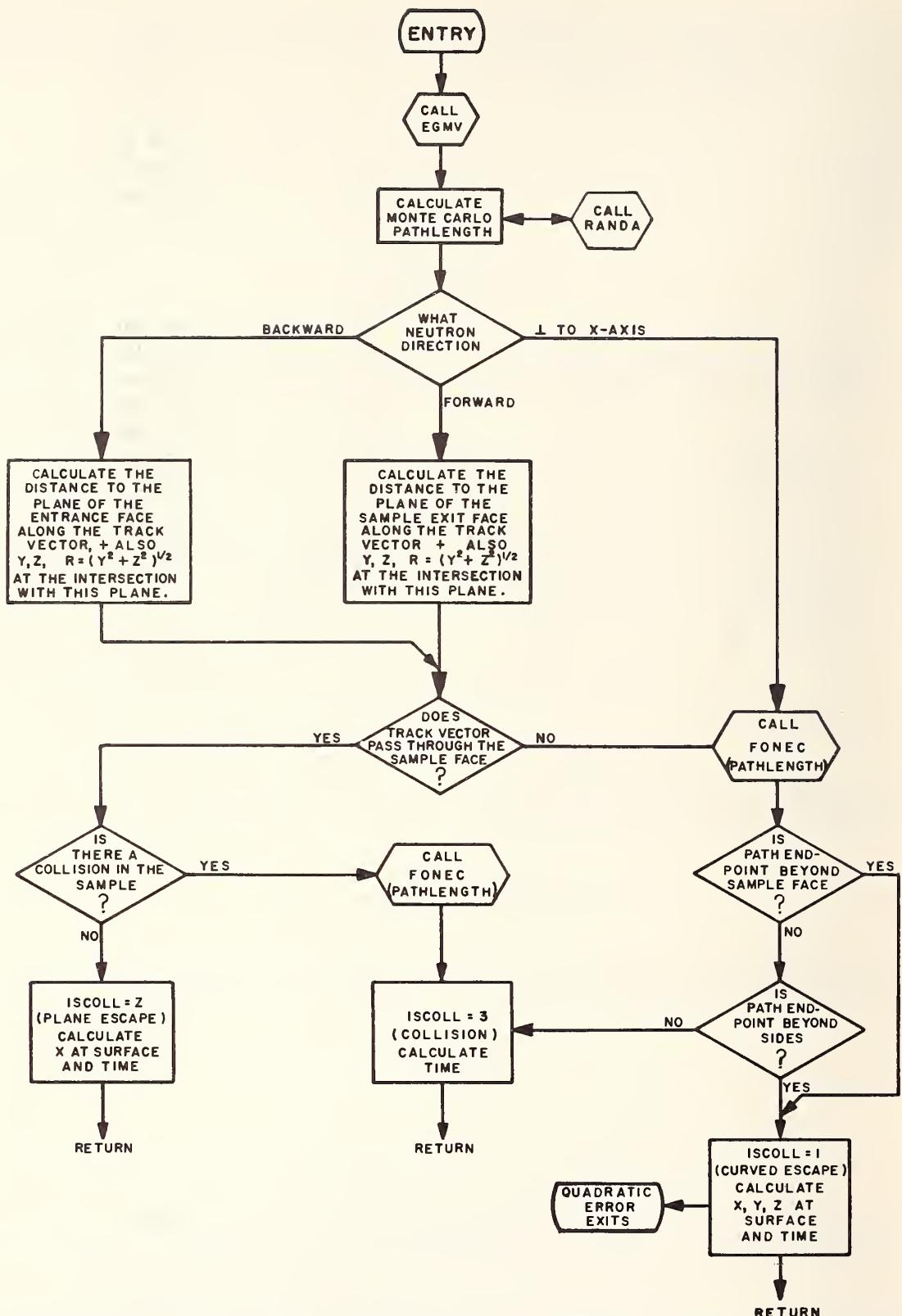


Fig. 4. Subroutine TRACK. The subroutines EGMV and FONEC return the neutron mean free path and the coordinates at the end of a track, respectively. RANDA returns a random number.

z coordinates. Error prints are provided for the cases of two positive, two negative, imaginary, or indeterminate roots as solutions to eq. (3). However none of these situations has occurred in many tens of thousands of tracks, although at least some of them are mathematically possible. Once ℓ has been calculated, determination of the coordinates of escape and the track time are straightforward. The subroutine also returns an index that indicates the fate of the neutron, i.e., curved escape, plane escape, or collision. A block diagram is shown on figure 4.

4. F PATH

This subroutine has also been entirely replaced. The same simplifying assumption is made as in the original coding--that is, the dimensions of the scattering sample are considered to be negligible compared to the flight path to the detector. This has the effect that the angle and flight path to any particular detector position may be considered to be the same from any scattering point in the sample. The quantities to be calculated are the neutron path length, p , in the sample from any point (x, y, z) to the surface of the sample and the scattering angle, θ_d , in the direction of a particular detector, at the angle ψ . The geometry is shown in figures 5 and 6. All paths are assumed to be parallel to the x - y plane, and all detector positions satisfy the condition $y \geq 0$.

We note that the locus of the intersection of a cone with a plane parallel to its axis is an hyperbola, and write, using the notation shown in figure 5,

$$\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1 \quad ,$$

$$\text{or} \quad y^2 = x^2 \tan^2 \theta - z \quad , \quad (4)$$

$$\text{since} \quad b = z \quad \text{and} \quad a = z/\tan\theta.$$

Now, referring to figure 6, we may also write

$$Y = p \sin\psi + y$$

$$\text{and} \quad X = p \cos\psi + x' \quad , \quad (5)$$

$$\text{where} \quad x' = R + h + x = \frac{r_1}{\tan\theta} + h + x.$$

Again we reduce the problem to a quadratic in path length, p , after

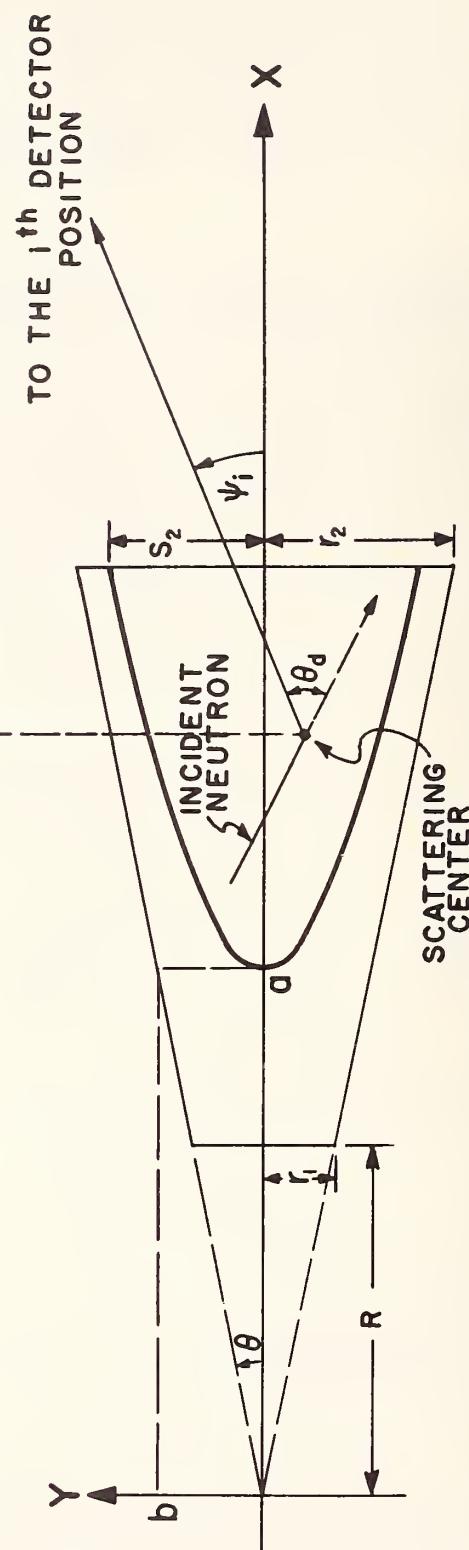
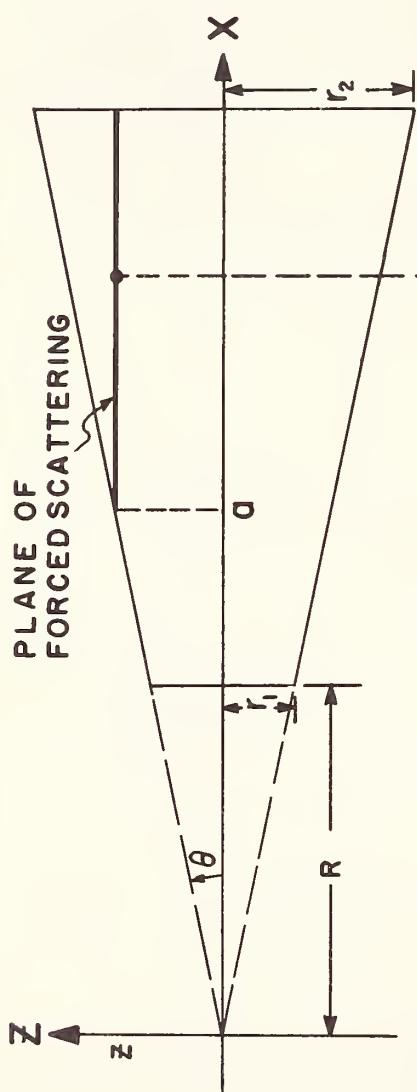
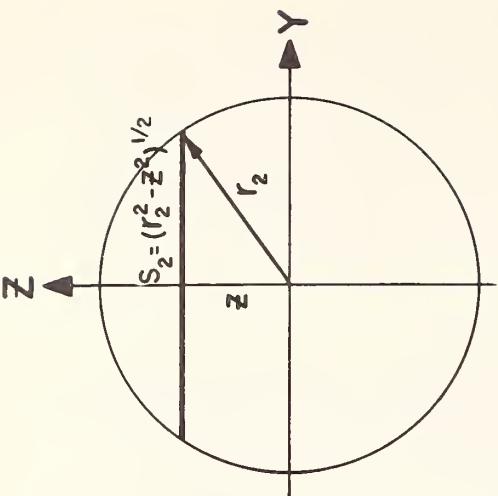


Fig. 5. The geometry for subroutine EPATH. The plane of forced scattering is located at a height $r_1 < z < r_2$ in this instance. The track of the incident neutron does not, in general, lie in this plane as shown.

TO THE i^{th} DETECTOR POSITION

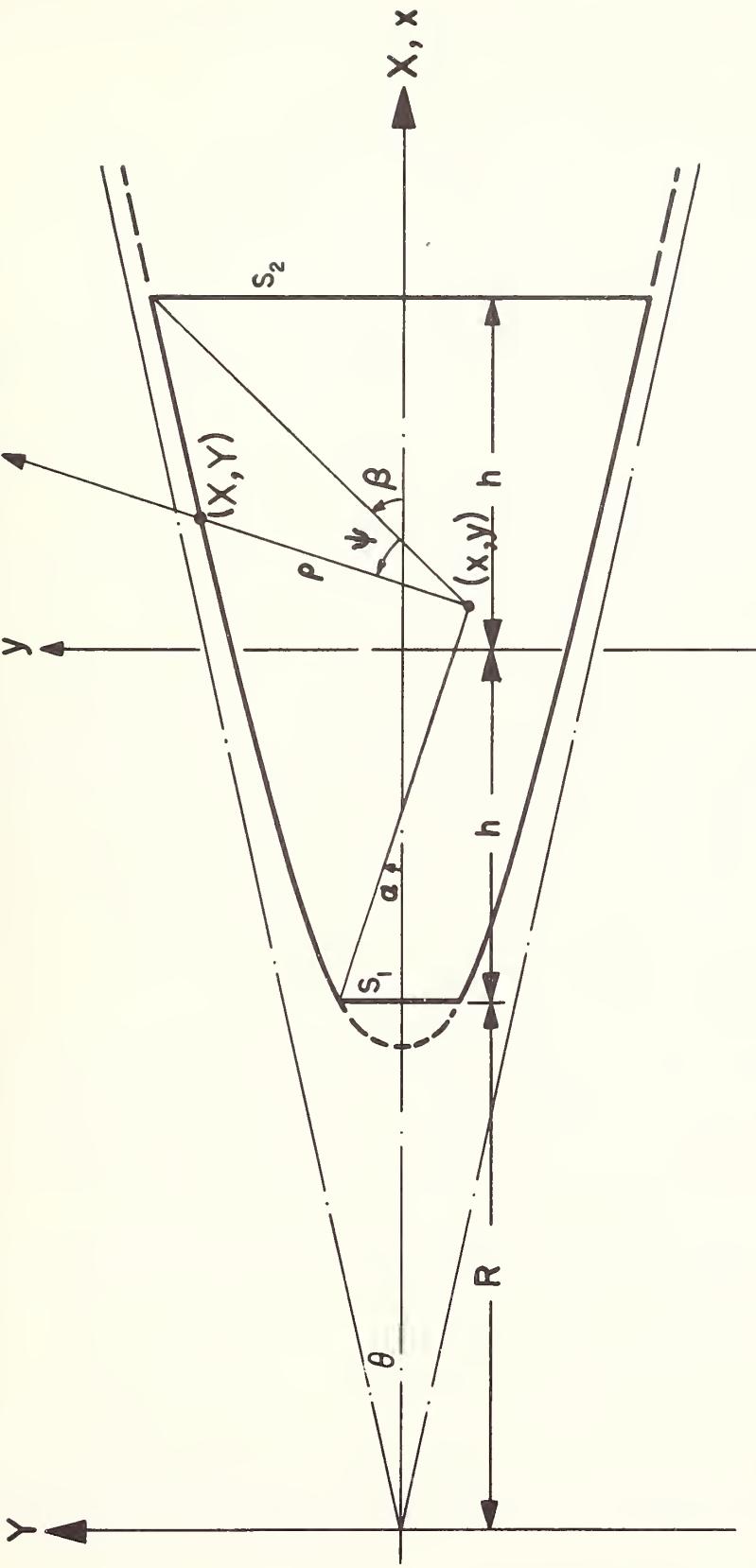


Fig. 6. A section through the scattering sample at height $z < r_1$. The upper case quantities refer to the axes X and Y , whose origin is that of hyperbola defined by the intersection of the plane (x,y) with the surface of the scattering sample.

combining eq's (4) and (5) to eliminate the variables X and Y to obtain:

$$\begin{aligned} & p^2 (\sin^2 \psi - \cos^2 \psi \tan^2 \theta) \\ & + 2p(y \sin \psi - x' \cos \psi \tan^2 \theta) \\ & + (y^2 - x'^2 \tan^2 \theta + z^2) = 0 . \end{aligned} \quad (6)$$

For each value of z there will be a pair of angles, α and β (see figure 6), which define the limits of the hyperbolic curve. These angles are given by

$$\begin{aligned} \tan \alpha &= \frac{(r_1^2 - z^2)^{1/2} - y}{h + x} \\ \tan \beta &= \frac{(r_2^2 - z^2)^{1/2} - y}{h - x} . \end{aligned} \quad (7)$$

The subroutine is diagrammed in figure 7. After testing for the special case of exit perpendicular to the beam axis, the program tests, using eq's (7), for exit through the endfaces vs. the curved sides for the exit angle, ψ , and branches accordingly. The path length in the former case is a straightforward calculation, and for curved escape is the positive root of eq. (6). It should be noted that in the limiting case of cylinder ($\tan \theta = 0$) this subroutine, unlike all of the others, does not work. A modified subroutine for a cylindrical sample is given in the Appendix following the listing of FPATH for a truncated cone.

B. Correction of Coding Errors [7]

1. INPUT

a. Statements resulting in $LGR=0$ in the table look-up for the mean free path (following card 0308) have all been changed to give $LGR=1$. $LGR=0$ references not a mean free path, but instead the last tabular value of collision probability in the previous MOULD table. The revised look-up supplies the mean-free path at the lowest tabulated energy for any neutron at or below that energy.

b. On the card following statement 5001, LRG has been replaced by the correct variable, LGR.

c. Card 0441 is replaced by

IMINM = IMAXM+1 .

This change yields sequential storage of supplementary ranges of experimental angular distributions, and thus avoids loss of needed storage space in the array SUPVAL(I,J).

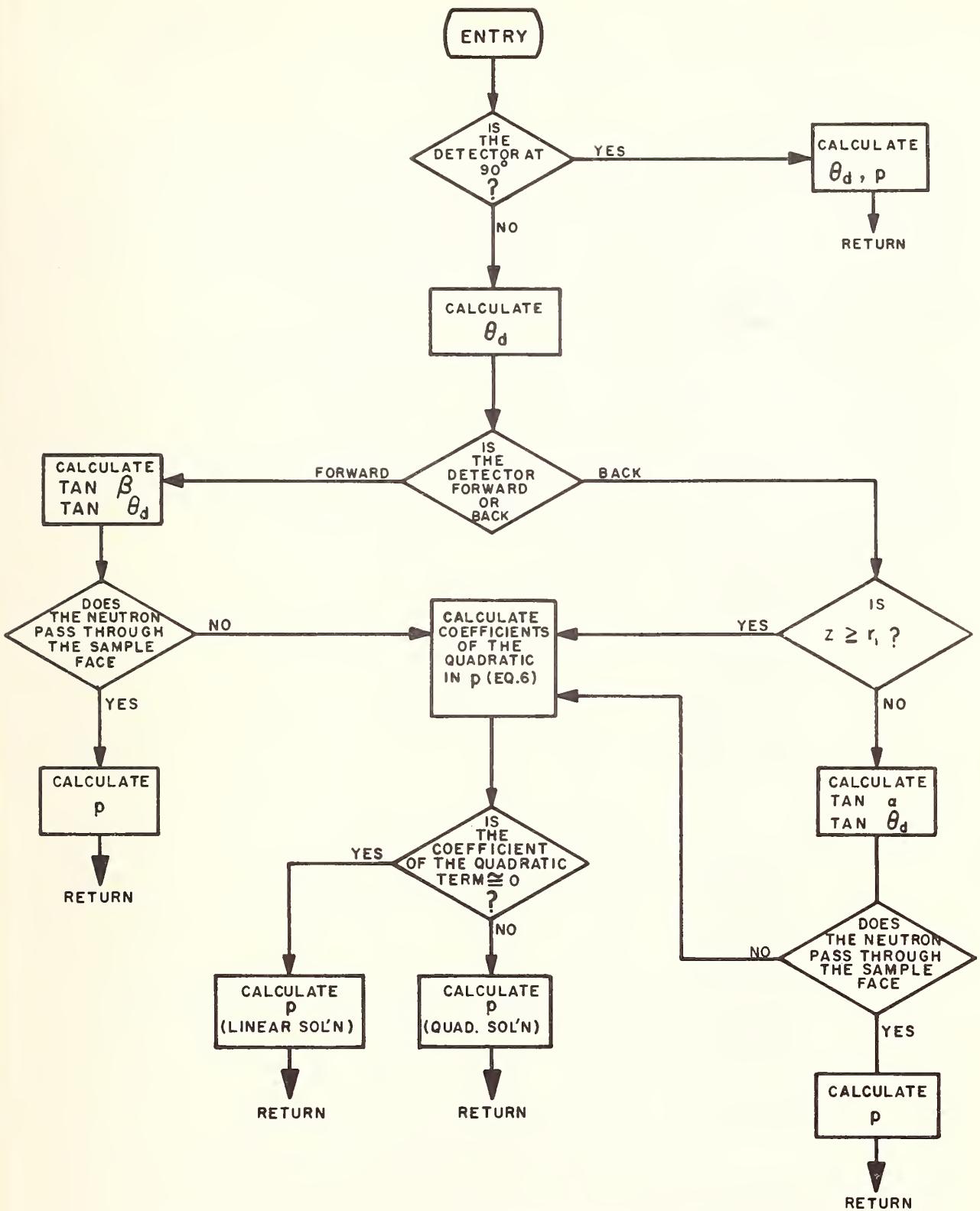


Fig. 7. Subroutine FPATH, for a truncated cone. The subroutine for a cylinder is similar.

2. EGMV

LGROUP=0 has been eliminated for the reason given in 1a. above.

3. NAPAN

a. The angle used for the interpolation of the experimental distributions, as well as for calculation of the neutron energy after collision is the laboratory angle, calculated in the subroutine FPATH. For this reason the experimental angular distributions must be read in at laboratory angles. Also the center-of-mass energy calculation on cards 3494 and 3497-3501 (in the case of center-of-mass MOULD angular distribution tables) is in error. This has been changed to a calculation in laboratory coordinates by replacing card 3494 by

GO TO (36,11,11,11,11,11,11,11,36,11,11,11,11,11,11) NFORM

and deleting cards 3497-3501.

b. The sequence of cards 3502-3512, which picks the appropriate experimental angular distribution values, does not refer to the correct angular distributions, nor to the correct neutron energy--that before collision. It has been replaced by the sequence:

```
11      IF(IMAX(J).LE.0) GO TO 15
        IMINM=IMIN(J)
        IMAXM=IMINM+IMAX(J)-1
        DO 50 JJ=IMINM,IMAXM
        IF(EIN-ENVAL(J,JJ)>50,51,52
          50      CONTINUE
          51      KK=JJ
          GO TO 19
          52      IF(JJ.LE.IMINM) GO TO 15
                    KK=JJ-1
```

c. On the card following statement 5001, LRG has been replaced by the correct variable, LGR.

d. LGR=0 has been eliminated for the reason given in 1a. above.

e. The option that provides for suppression of printout of various scores, through setting the indicators IANALA, IANALB, IANALC, and IANALD negative, should not suppress storage of these scores by NAPAN. The time saved is negligible and the elastic scores, DEB(I,L), are required by the automatic iteration scheme, AUTO. Cards 3528-43 have been revised to eliminate the dependence on these printout indicators.

4. ABSYND

LGROUP=0 has been eliminated for the reason given in 1a. above.

5. CREN

For the same reason set out in section 3a. above, the center-of-mass energy calculation (cards 2960-66) has been replaced by a calculation in laboratory coordinates by deleting cards 2961-66 and replacing card 2960 with

880 GO TO 800 .

6. OUTPUT, OUTB3, OUTB4

The sum over energy, at each detector angle, stored in the vector DES(J,33) is required by subroutine AUTO. So as to allow calculation of this quantity in subroutine OUTB4, even when no B4 printout is requested, a print indicator, IFPR, has been added to the call for subroutine OUTB4. This is accomplished by the changes shown in the listing for cards 3721, 3808A, 3873, and 3975-4002.

7. AUTO

a. The quantity "chi-squared," on card 2084, should be

$$\chi^2 = \sum_{j=1}^{33} \frac{\left(\sigma(\theta_j) \exp^{-\chi(\theta_j)} \text{calc} \right)^2}{\sigma(\theta_j) \exp},$$

and not as formerly written, with the denominator squared.

b. It should be noted that the normalization of the Monte Carlo output on cards 2065-2068 and 2088 is not, in general, correct; but only holds for detectors positioned at equal increments of $\cos\theta$ between -1 and +1. For this reason, if subroutine AUTO is used, the input detector positions must satisfy this criterion.

8. FPATH

The original version of this subroutine contained two errors. These do not apply to the new version of FPATH reported here, but are listed for completeness. Card 3356 of the original should read

SINOM = SQRT(1-COSOM**2) ,

card 3358 be deleted, and a new card inserted following card 3359:

FP1 = WORK16**2+WORK17**2-FP2**2 .

C. Other Modifications

1. General

a. Common storage assignments have been handled by combining all common statements into one package, processed by the UNIVAC 1108 "Procedure Definition Processor" using the assembler directive FCOPY (Fortran copy). This package, designated CINC1, is then included at the time of assembly in all subroutines making use of common variables by means of the statement

```
INCLUDE CINC1
```

placed immediately following the subroutine name definition. This process, which effects a considerable economy in the size of the source deck and listing, is characteristic of the UNIVAC 1108 Assembler and FORTRAN V; however, equivalent procedures are often available to other systems. In some subroutines dimension statements still appear for those few variables not in common storage. A block of common storage has been specifically assigned to the subroutine ABSYND variables DATA and IDATA. This carries the dummy label BLANK. The details of these changes in memory storage allotment will be obvious upon examination of the listings.

b. The size of many modern computers obviates the need for linkage. We have deleted references to CHAIN(I,J) and incorporated the balance of subroutine PRELUDE into the main program MAGGIE. Similarly, references to CHAIN(I,J) in subroutines DATIN and AUTO have been replaced by the appropriate CALL and/or RETURN statements.

c. The final F in the names of all library functions (such as SIN, COS, EXP, MIN) has been deleted, as it is not compatible with FORTRAN V. In addition, such functions as FLOAT and INT have been eliminated by using the mixed expressions allowed by FORTRAN V.

d. Disc storage read and write statements have been modified in the main program MAGGIE and subroutine WRTBT to conform to 1108 FORTRAN V usage.

e. A number of formats have been altered. Some of the changes are merely different spacing options, but others are required by the new scattering geometry. A list of card numbers of the affected statements follows:

0226	0226A	0226B
0249	0258	0345
0410	0450	0451
1719	1963	1972
2111	2115	3638
3639	3828	3833

On card 2735 in subroutine CR the variable N has been replaced by the correct variable NSECS.

f. A new random number generator, subroutine RANDOM, entry RDM, has been incorporated, and the required changes in the functions RANDA and NRANDA are shown in the listings.

2. MAGGIE

a. All of the subroutine PRELUDE, except for calls to subroutines CLOCK and CHAIN, has been inserted following card 1654. A call to subroutine RANDOM immediately following the read-in of OCT, the starting value of the random number generator, initializes this generator. OCT is printed out following the call to subroutine INPUT.

b. All references to subroutine CLOCK have been deleted.

c. Card 0530 is eliminated by changing cards 1776, 1778, 1787, 1789, and 1792 to read

GO TO 1 .

3. ABSYND

a. Card 0525, which assigns the logical tape unit carrying the MOULD nuclear data tape, now reads

NUCDAT=9 .

On cards 0525, 0530, and 1394 the variable name TAPE has been changed to ATAPE to avoid confusing the compiler. These changes may not be required by other installations.

b. Cards 0553 and 0554 set all storage for the variables DATA and IDATA to zero before each ABSYND run.

c. Card 1398 is modified so as to print only those action numbers processed.

4. CR

The variable names NACT and Q have been changed to NACTV and QV, so as to avoid conflict with the array names NACT(I) and Q(I). Similarly, the variable name COS is changed to COZ, so as to make the library function COS available.

5. CREN

a. The variable names NACT and Q have been changed to NACTV and QV, for the reason given above.

b. Cards 2832-2837, 2878-2881, and 2911-2915 have been deleted, since they are not needed. In order to accomodate these deletions card 2910

has been amended to read

IF(NVCOS.LT.1) GO TO 208

,

and card 2916 to read

P = (AS+SQRT(AS**2+A*QV*(1+A)/EIN+A**2-1))/(1+A) .

6. AUTO

a. The multiple elastic sums are not required, and so cards 2069-2072 are deleted.

b. The quantity RATIO is not used, and has been eliminated from cards 2077 and 2078.

c. The do-loop 2083-2085 is redundant, since ELM2(J) is also set at card 2097. Cards 2083-2085 are therefore deleted, and card 2080 is modified to reflect this change.

d. The three do-loops in the sequence 2087-2098 have been combined into a single loop.

e. The variable name EXP(J) has been changed to EZP(J) to avoid conflict with the library function EXP.

f. Often it is desirable to separate an iteration procedure into two or more consecutive runs. Cards 2073-2082 have been modified to allow a run to be made using the partially corrected output of a previous run as input, instead of the experimental data. When this option is to be used the second field of the input card specifying the number of iterations, NTERM, should be non-zero. This is then followed by the cards specifying the experimental values for the angular distribution, FCVAL, which are removed from their usual position and replaced by the partially corrected output of the previous run.

g. In the case of rapidly varying angular distributions such as at 14.1 MeV, the usual iteration procedure is not as rapidly convergent as the "physical" method. For this method the calculated multiple scattering is first subtracted from the experimental input, and then the balance of the iteration (sample attenuation) is performed as usual by reflecting the output for single scattered neutrons about the input. The new coding on cards 2091-2097 reflects this change. For the first two iterations the iteration improves only the multiple scattering, the correction being applied both times to the experimental input. After two iterations multiple scattering is well enough known to allow the iterative procedure full play, so the correction is applied each time to the previous input, instead of the experimental values. This procedure yields much more rapid convergence, three iterations providing better convergence than six of the previous method.

III. AN APPLICATION TO 14.1 MeV NEUTRON SCATTERING

The code has been applied to a typical associated-particle scattering geometry for 14.1 MeV neutrons on carbon. The scattering sample was a truncated cone of half-angle seven degrees, length 3.193 cm., and entrance face radius 2.059 cm., with its center located 20 cm from the neutron source. The experimental input used was simulated using published results for carbon at this energy. The results of a typical run are shown in Table 1, and on figures 8 and 10. The cross-section data used for the Monte Carlo scattering were those of Slaggie and Reynolds [8]. In Table 1 the quantity $\sigma(\theta)$ represents the true angular distribution, and the total and multiple outputs are the results calculated using it and the specified sample shape. The code varies $\sigma(\theta)$ until the total elastic output matches the experimental input to the accuracy required. The calculated angular distribution for neutrons undergoing multiple scattering is shown in figure 8. It can be seen that the result converges quite rapidly. Further iterations resulted only in statistical variations about the values obtained after three iterations; in fact, the largest change after two iterations, that at $\cos \theta = 0.625$, represents only a 1.5% change in the cross section.

In figure 9 we show the part of the correction, exclusive of multiple scattering, that depends upon sample shape. Also displayed for comparison is a calculation of the effect expected due to attenuation in the sample for an isotropic angular distribution. As can be seen, this correction is not independent of the input angular distribution. The quantity plotted, $\Delta\sigma/\sigma$, is the difference between the singly scattered output and the input, divided by the input, for each angle. This geometrical correction is contributed to about equally by varying path length in the sample and the change in the total neutron cross section with energy as a function of the neutron scattering angle. The correction varies from a few percent to about ten percent, and is directly dependent upon the accuracy with which the total neutron cross section is known over the range of energy exhibited by the neutron recoil. On the other hand, the correction for multiple scattering is larger, ranging from about 50% at the backward minimum to 4% at zero degrees, but depends mainly upon the experimental input data. Over most of the practical angular range of measurement it is a quite appreciable 15-20%. Figure 10 shows the input distribution used and the corrected output distribution obtained after three iterations of approximately 2000 interacting neutrons each. The total correction is, of course, largest in regions where the cross section exhibits minima. It varies from a few percent to a maximum of only twenty percent at measurable angles, since the geometrical and multiple scattering corrections tend to be in opposite directions, except at the extreme backward angles. Several examples of spectra showing elastic-inelastic and multiple inelastic effects in the energy spectra are given in the original references [4, 5]; the present version of MAGGIE also yields similar results.

TABLE 1

The scores for a typical Monte Carlo run for carbon at 14.1 MeV.

COUNTER NUMBER	COS θ	$\sigma(\theta)$	TOTAL ELASTIC OUTPUT	MULTIPLE ELASTIC OUTPUT	EXPERIMENTAL INPUT
1	-1.0000	.023	.044	.021	.044
2	-.9375	.075	.092	.022	.093
3	-.8750	.093	.111	.024	.111
4	-.8125	.100	.120	.026	.121
5	-.7500	.110	.131	.028	.131
6	-.6875	.127	.148	.030	.148
7	-.6250	.152	.170	.031	.171
8	-.5625	.176	.190	.033	.191
9	-.5000	.202	.212	.034	.212
10	-.4375	.225	.231	.035	.232
11	-.3750	.240	.246	.036	.246
12	-.3125	.248	.253	.037	.254
13	-.2500	.245	.251	.037	.251
14	-.1875	.233	.240	.038	.241
15	-.1250	.216	.225	.038	.226
16	-.0625	.192	.205	.038	.205
17	.0000	.173	.183	.038	.183
18	.0625	.145	.155	.037	.155
19	.1250	.125	.135	.037	.135
20	.1875	.114	.125	.037	.125
21	.2500	.107	.123	.039	.122
22	.3125	.110	.127	.041	.126
23	.3750	.124	.142	.044	.140
24	.4375	.154	.170	.049	.167
25	.5000	.203	.215	.055	.212
26	.5625	.281	.285	.063	.281
27	.6250	.412	.404	.074	.400
28	.6875	.628	.605	.087	.600
29	.7500	.969	.929	.104	.925
30	.8125	1.486	1.435	.125	1.435
31	.8750	2.274	2.218	.151	2.219
32	.9375	3.451	3.380	.181	3.387
33	1.0000	5.197	5.045	.216	5.062

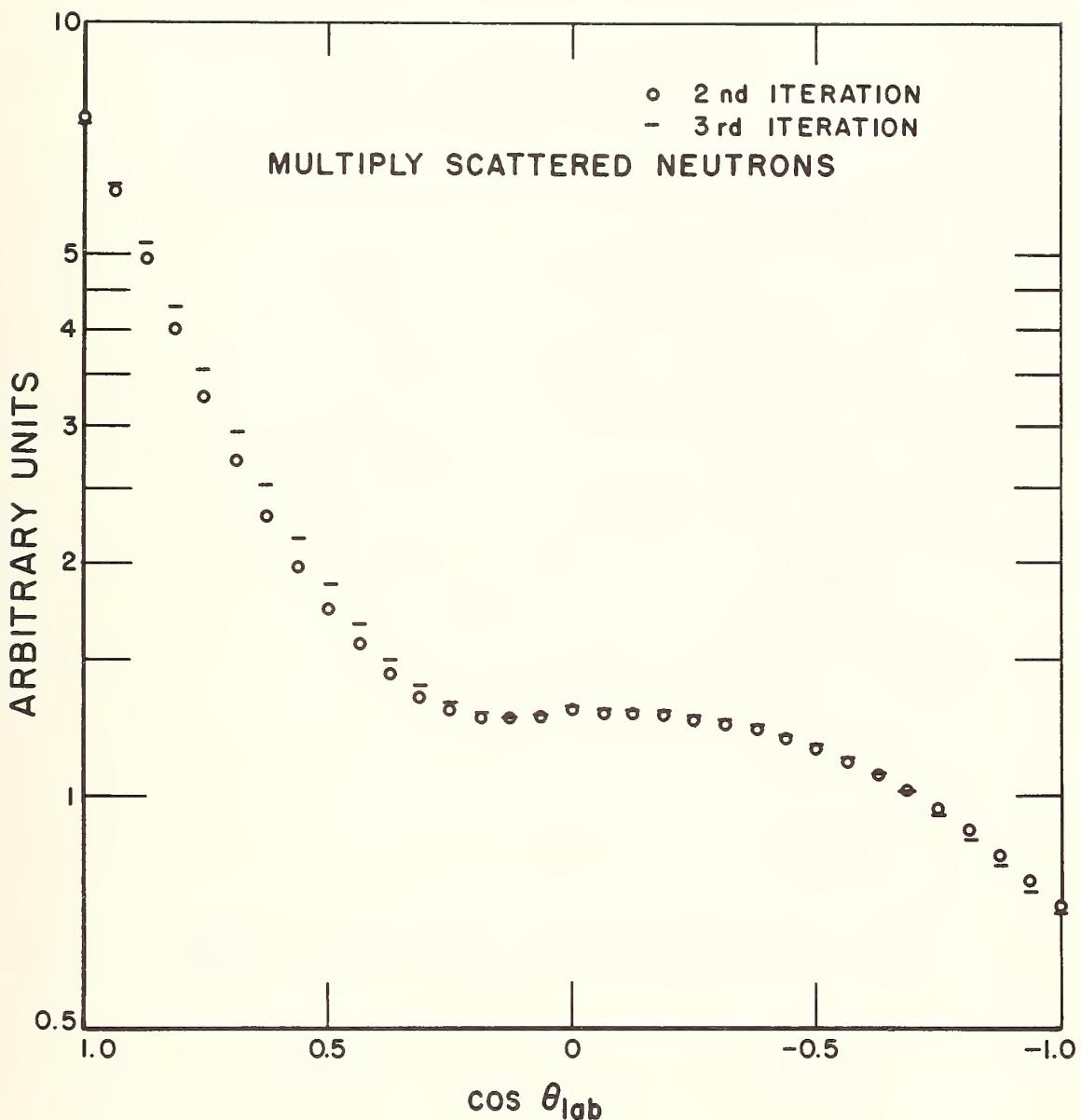


Fig. 8. The angular distribution of multiply scattered neutrons on carbon at 14.1 MeV for two successive iterations. The data for the third iteration are also given in Table 1, after suitable normalization.

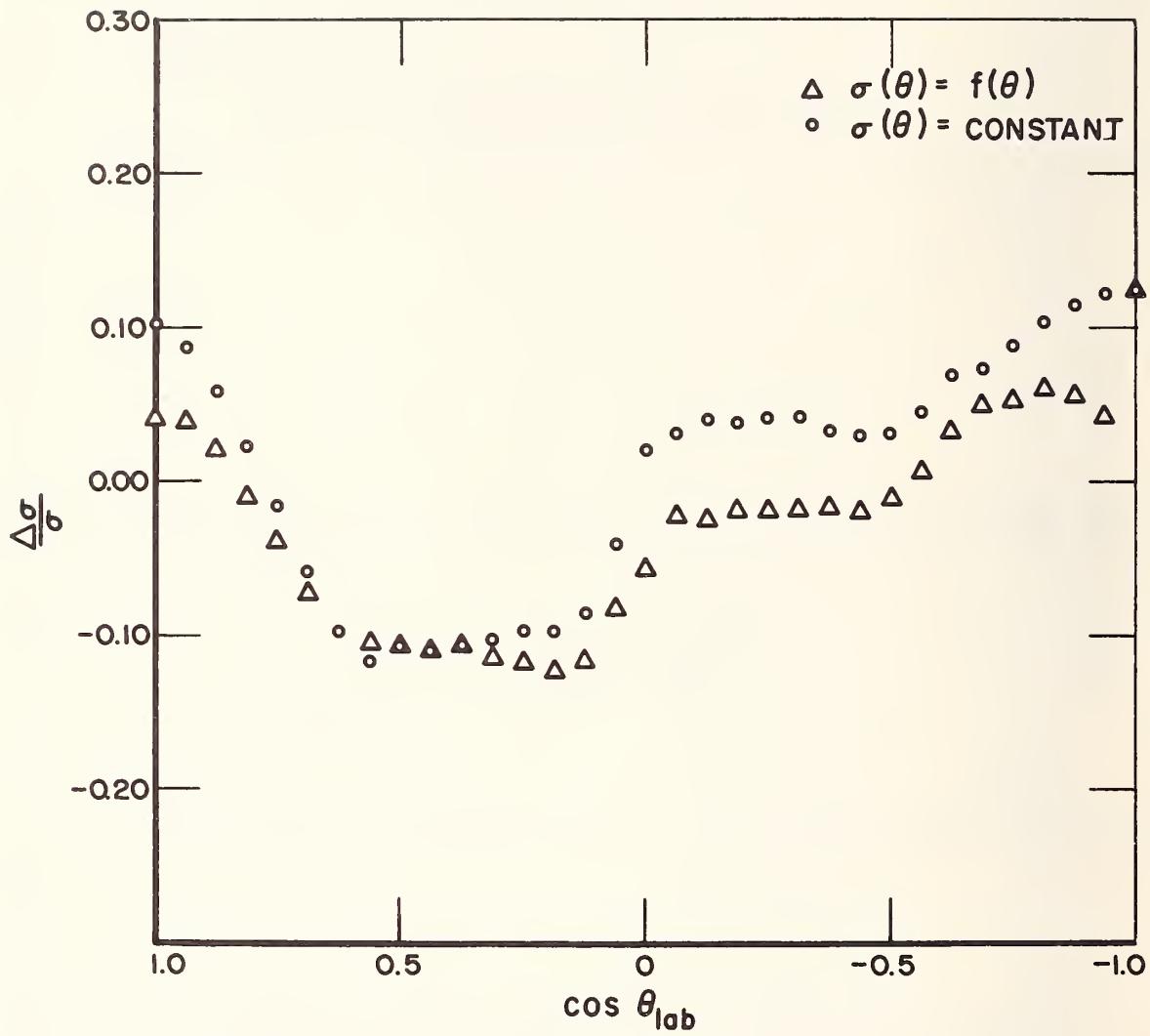


Fig. 9. The correction due to sample shape. The quantity $\Delta\sigma/\sigma$ is the change in the normalized angular distribution after subtracting multiple scattering.

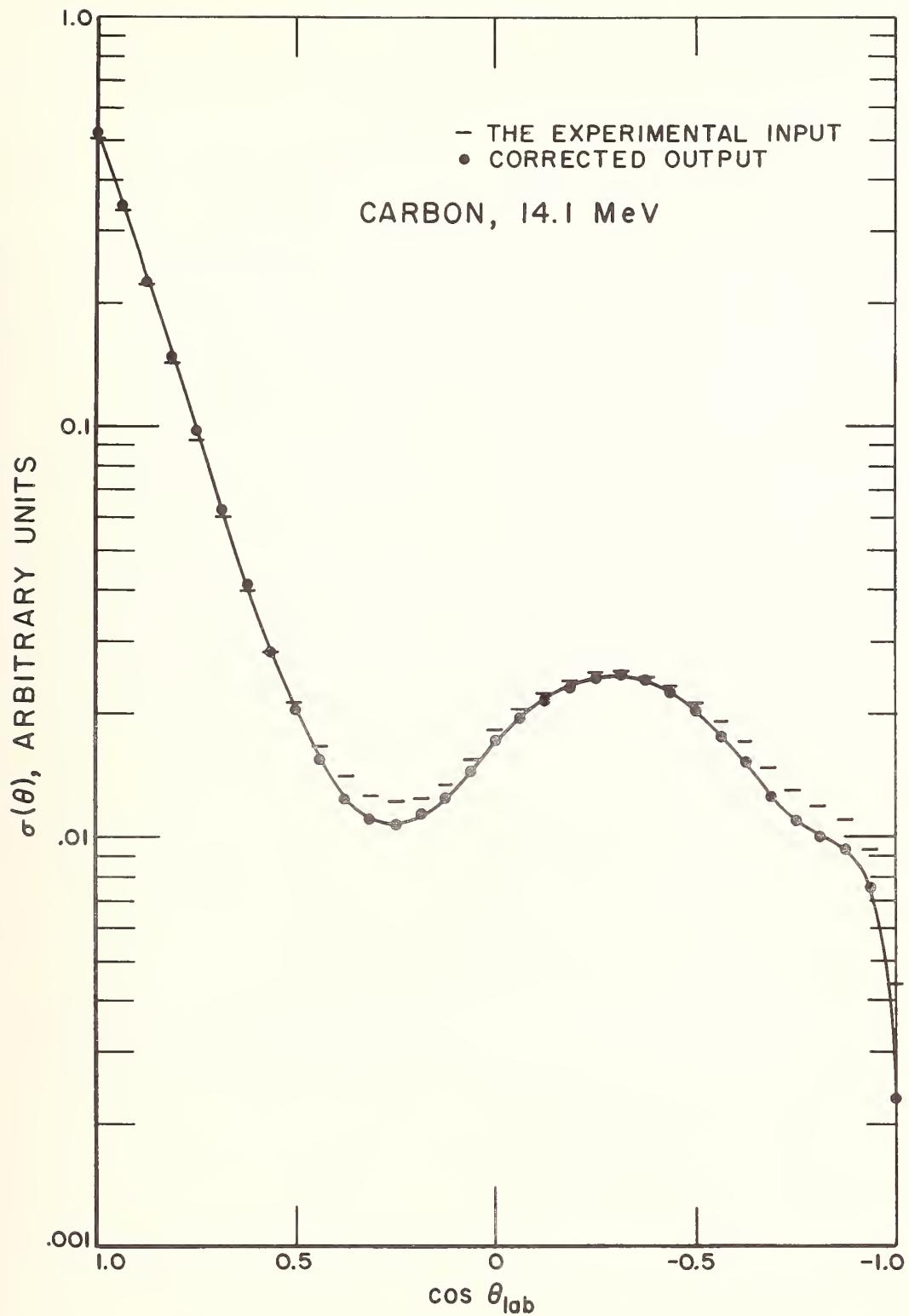


Fig. 10. The experimental input and corrected output for carbon at 14 MeV.

REFERENCES

1. Monier, L. F. C., Tripard, G. E., and White, B. L., Nucl. Instr. and Meth. 45, 282 (1966).
2. Marshak, H., Richardson, A. C. B., and Tamura, T., Phys. Rev. 150, 996 (1966).
3. A useful summary is given by M. Walt in Fast Neutron Physics, Vol. II, Marion, J. B., and Fowler, J. L., Ed. (1960).
4. Parker, J. B., Towle, J. H., Sams, D., and Jones, P. G., Nucl. Instr. and Meth. 14, 1 (1961).
5. Parker, J. B., et al, Nucl. Instr. and Meth. 30, 77 (1964).
6. Parker, K., AWRE report 0-70/63; Kerr, W. M. M., AWRE report 0-81/64 (1964); Miller, S. M., and Parker, K., AWRE report 0-55/65.
7. Some of these coding errors have also been previously noted in private communications. We are indebted to J. B. Parker, Aldermaston, for noting the substitution of REDEN for EIN in subroutine NAPAN, as well as the errors in subroutine FPATH. H. Horstmann and H. Schmid, Geel, have noted, in addition, the difficulty involving the center of mass calculation of neutron recoil energy in subroutines NAPAN and CREN.
8. Slaggie, E. L., and Reynolds, J. T., KAPL-3099, (1966).

APPENDIX A

Listings of new and extensively revised coding.

<u>Name</u>	<u>Page</u>
CINC1	28
MAGGIE 3A	30
INPUT	36
CRNEU	44
TRACK	46
NAPAN	49
FPATH (truncated cone)	53
FPATH (cylinder)	55
OUTPUT	56
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RANDOM	61
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A complete listing is available by request from the Center for Radiation Research, Neutron Physics Section, National Bureau of Standards, Washington, D. C. 20234.

```

CINC1* FCOPY          NBS
C                           EU.
C                           EU.
C                           EU.
C                           NBS
C COMMON STORAGE ALLOCATION.
C
C COMMON LOC,OCT          EU.
C DIMENSION DATA(1),IDATA(1) EU.
C EQUIVALENCE (DATA, IDATA) EU.
C COMMON IDATA,INIT,NEGS,UMAX,XLYMIN,IXMAT,IDIICE,NMATS,EMC(257),
C PATH,SPEED,MAT,EIN,UIN,LGROUP,ROOTE,WIN,WOUT,NSECS,      NBS
C 1 COSPHI(100),EOUT(100),UOUT(100),ISORAN(100),NOLAW(100), NBS
C 2 NONUC(100),NOACT(100),NREACT(100),NORNGE(100),ALF,      NBS
C 3 ALFP(20),WMIN,WMAX   NBS
C 4
C
C MAGGIE NUCLEAR DATA AIDS.          EU.
C
C COMMON NUCLID,NAC,AS,ENER,INFORM,QV,ATOM1(24),Q(24),PART1(24),    NBS
C IXACT1(24),IXNUC1,FNEGS,NUCS,NUCL(24),NACT(24),NAC1(24),    NBS
C NANAL,NENSP,NOCOU,NOGR,LAWREV(50),LWNO(50),NLWREV        NBS
C
C BIRTH STORES AND REGISTERS.          EU.
C
C COMMON BIRTH(5500),IBIRTH(15000)     EU.
C
C GENERAL WORK STORES.               EU.
C
C COMMON IWORK1,IWORK2,WORK3,WORK4,WORK5,WORK6,WORK7,WORK8,WORK9,    NBS
C 1 WORK10,WORK11,WORK12,WORK13,WORK14,WORK15,WORK16,WORK17,    NBS
C 2 WORK18,WORK19,ISCOLL             NBS
C
C DIMENSIONS ETC.                  EU.
C
C COMMON HITE,FRAD,BRAD,ANGLE,TANGLE,DIST,STRTE,CNPPhi(64),FLTPTH  NBS
C
C CONTROL PARAMETERS.            EU.
C
C COMMON IRECRG,IRGRA,IRGRB,JOBFIN,NOSAMP,SAMPLE,ANEUNO,NSENSE,IFB4  NBS

```

PAGE:

5

```
C ANALYSIS AND AIDS TO ANALYSIS.
C
C COMMON HEAD(12),ONCOL(31),DEGENE(30),DEGENI(30),EDGEN(30),
C 1 ICOL(100),AMISS,PESC,CESC,ANOCOL,ALLEL,EVDGEN,FCCOS(33),
C 2 FCCOSD(33),FCER(24,15),FCVAL(24,33),SUPVAL(24,33),
C 3 EIVAL(24,24),IMAX(24),IMIN(24),ENSP(33),COUNT(33),
C 4 TOCOL(5,5),
C 5 DEB(33,33),DEC(33,33),DED(33,33),IANALA,IANALB,IANALC,
C 6 IANALD,FLUXFT,ALAM(32),ITMAG,ITER,EZP(33),NTERM,SAMP(10)
C
C ABSYND IDATA AND DATA STORAGE
C
C COMMON BLANK(15000)
C
C END
```

```

C MAGGIE 3A 1566
C 20.7.64 A.D.PURNELL 1570
C 9.68 MODIFIED NBS VERSION FOR FORTRAN V. A.C.B.RICHARDSON NBS1570A
C FOR TRUNCATED CONE SCATTERING SAMPLE, INCLUDING AUTOMATIC ELASTIC NBS1571
C SCATTERING CALCULATION AND GRAPHS. NBS1571A

INCLUDE CINC1
DIMENSION LAWTP(100)
ITER=1 1653
INIT = 16719 1654
READ(5,51) OCT
CALL RANDOM(OCT)
51 FORMAT(0I12)
READ(5,200)(HEAD(I),I=1,12)
WRITE(6,200)(HEAD(I),I=1,12)
200 FORMAT(12A6)
CALL DAT IN
CALL INPUT
WRITE(6,52) OCT
52 FORMAT(5SHU)THE STARTING VALUE FOR THE RANDOM NUMBER GENERATOR IS
1012) 1656
103 NOSAMP=0
IRECRG=U
IRGRA=0
IRGRB=0
ANEUNO=0.0
THERM=0.25000001E-7
IF (IRGRA) 2,7,4
PRINT 3,ANEUNO
FORMAT(1H1,4THERROR CONDITION-BIRTH REGISTER NEGATIVE ANEUNO=.F6.0
2) 1658
IRGRA=0
IRGRB=0
GO TO 7
1 IRGRA=IRGRA-11
2 IRGRB=IRGRB-3
3
4

```

```

IWORK1=IBIRTH(IRGRB+1)
MAT=IBIRTH(IRGRB+2)
IWORK2=IBIRTH(IRGRB+3)
EIN=BIRTH(IRGRA+1)
WORK3=BIRTH(IRGRA+2)
WORK4=BIRTH(IRGRA+3)
WORK5=BIRTH(IRGRA+4)
WORK6=BIRTH(IRGRA+5)
WORK7=BIRTH(IRGRA+6)
WORK8=BIRTH(IRGRA+7)
WORK19=BIRTH(IRGRA+8)
UIN=BIRTH(IRGRA+9)
WIN=BIRTH(IRGRA+10)
WORK11=BIRTH(IRGRA+11)
IF(IRGRA-550)13,5,13
13(IF(IRECRG)13,13,6
IRECRG=IRECRG-11
LOC=LOC-5600
READ(37)IRECRG,BIRTH(I),I=551,4950),(IBIRTH(I),I=151,1350)
IREGRA=IRGRA+4400
IRGRB=IRGRB+1200
GO TO 13
13 IF(ANEUNO-SAMPLE)10,8,8
8 NOSAMP=NOSAMP+1
ANEUNO=0.0
CALL OUTPUT
IF(ITMAG-1)81,82,81
81 IF(NOSAMP-JOBFIN)10,9,9
82 IF(NAC1(1)-2)9,84,9
84 IF(NOCOU-33)9,85,9
85 CALL AUTO
IF(ITER-10)103,9,9
9 CONTINUE
CALL END
10 CALL CRNEU
IF(INSENSE)11,13,11
11
13
15
16
17

```

```

11 PRINT 12
12 FORMAT(120H$SERIAL STEP EN LETH WT L M N NBS1719
13 X Y Z TIME FATE ISO. ACT. RAN. LAW NSEC$) 1720
14 IF (NSENSE) 14,15,14 33,ANEUNO,IWORK1,EIN,UIN,WIN,WORK3,WORK4,WORK5 1721
15 PRINT 2,WORK6,WORK7,WORK8,WORK19 1722
16 CALL TRACK 1723
17 WORK1=WIN 1724
18 ISCOLM=ISCOLL 1725
19 GO TO (17,16,22),ISCOLM 1726
20 PESCE=PESC+WORK1 1727
21 GO TO 18 1728
22 CESC=CESC+WORK1 1729
23 IF (NSENSE) 19,20,19 1730
24 PRINT 34,ANEUNO,IWORK1,EIN,UIN,WIN,WORK3,WORK4,WORK5 1731
25 WORK16,WORK17,WORK18,WORK19,ISCOLM 1732
26 CONTINUE 1733
27 505 IF(IWORK1)506,506,507 1744
28 506 ANOCOL=ANOCOL+WORK1 1745
29 GO TO 1 NBS1746
30 507 IF (IWORK1-1)1,508,509 NBS1747
31 508 I=ICOLL(1) 1748
32 ONCOL(I)=ONCOL(I)+WORK1 1749
33 GO TO 1 NBS1750
34 NOIN=0 1751
35 DO 511 I=1,1,WORK1 1752
36 IF (ICOLL(I)-2)511,511,510 1753
37 NOIN=NOIN+1 1754
38 LAWTP(NOIN)=LAWTP(I) 1755
39 CONTINUE 1756
40 IF (NOIN=2)518,512,518 1757
41 IF (LAWTP(I)-LAWTP(2))513,514,514 1758
42 I=LAWTP(2) 1759
43 J=LAWTP(1) 1760
44 GO TO 515 1761
45 I=LAWTP(1) 1762

```

```

J=LAUTP(2)          1763
515  IF(I-5)=516,518 1764
      IF(J-5)=517,518 1765
516  TOCOL(I,J)=TOCOL(I,J)+WCRK1 1766
517  IF(ICOLL(I)-2)=524,519,519 1767
518  J=ICOLL(I)-1 1768
519  NOIN=0 1769
      DO 521 I=1,1WORK1 1770
      IF(ICOLL(I)-2)=521,520,520 1771
      NOIN=NOIN+1 1772
520  CONTINUE 1773
      IF(NOIN-1)=522,523 1774
      DEGENE(J)=DEGENE(J)+WORK1 1775
521  GO TO 1 1776
      DEGENI(J)=DEGENI(J)+WORK1 1777
      GO TO 1 1778
      NOIN=0 1779
      DO 526 I=1,1WORK1 1780
      IF(ICOLL(I)-2)=526,525,525 1781
      NOIN=NOIN+1 1782
      NOIN1=ICOLL(I) 1783
522  CONTINUE 1784
      IF(NOIN-1)=527,529,528 1785
      ALLEL=ALLEL+WORK1 1786
523  GO TO 1 1787
      EDGENE=EDGENE+WORK1 1788
524  GO TO 1 1789
      NOIN1=1 1790
      EDGEN(J)=EDGEN(J)+WORK1 1791
525  GO TO 1 1792
      NOIN=1 1793
      COLSN 1794
      1WORK1=1WORK1+1 1795
526  CALL CR 1796
      IF(IFB4)=23,24,23 1797
      1798
      1799

```

```

23      CALL CALC
        CALL NAPAN
        WORK1=UOUT
        IF(IWORK1-100)25,25,26
24      IF(IREACT(1)-2)532,531,532
25      ICOLL(IWORK1)=1
        IF(IWORK1-1)26,5310,26
5310    ALAM(1)=ALAM(1)+WORK1
        GO TO 26
26      IF(NREACT(1)-16)534,533,533
532     ICOLL(IWORK1)=2
        ICOLL(IWORK1)=2
        IF(IWORK1-1)26,5330,26
533     ALAM(2)=ALAM(2)+WORK1
        GO TO 26
5330   DO 535 1=1,NLWREV
        IF(ROLAN(1)-LAWREV(1))535,536,535
534     CONTINUE
        ICOLL(IWORK1)=3
        LAWTP(IWORK1)=1
        IF(IWORK1-1)26,5350,26
5350   ALAM(3)=ALAM(3)+WORK1
        GO TO 26
536     ICOLL(IWORK1)=ELWNO(1)+3
        LAWTP(IWORK1)=ELWNO(1)+1
        IF(IWORK1-1)26,5360,26
5360   ALAM(1+3)=ALAM(1+3)+WORK1
        IF(NSECS)32,507,27
27      WORK10=UOUT
        DO 31 1=1,NSECS
          WORK12=LOUT(1)
          WORK9=UOUT(1)
          IF(WORK12-THERM)28,29,29
28      WORK9=LOG(THERM/0.25E-7)
29      ANGLE=COSPHI(1)
        CALL TWIST(ANGLE)

```

```
CALL WR1BT  
IF(NSENSE)30,31,30  
PRINT  
2WORK14,WORK15,WORK16,WORK17,WORK18,WORK19,WORK20,  
3,NORNGE(I),NOLAW(I),NSECS  
CONTINUE  
31  
60 TO 1  
32 FORMAT(1H0,F7.0,I4,9F7.3,F10.4,I5,3I6,I5,I7)  
33 FORMAT(1X,F7.0,I4,9F7.3,F10.4,I5,3I6,I5,I7)  
34  
END
```

SUBROUTINE INPUT

```

C          0123
C          0204
C          GENERAL INPUT FOR TRUNCATED CONE, INCIDENT NEUTRONS ALONG THE AXISNBS0205
C          0206
C          INCLUDE CINCI
C          DIMENSION STDIST(25),ANGS(25),AREA(25),NOACA(24)
C          READ(5,201)IFB4,NSENSE
C          READ(5,202)HITE,FRAD,ANGLE
C          WRITE(6,204)HITE,FRAD,ANGLE
C          FORMAT(4HUTHE SCATTERER IS A TRUNCATED CONE OF LENGTH =,F7.3,
C          127HCMS, ENTRANCE FACE RADIUS =,F7.3,21HCMS, AND HALF ANGLE =
C          2F7.5,8HRADIANS.)
C          HITE=HITE/2.
C          READ(5,201)JOBFIN,ITMAG
C          READ(5,202)           SAMPLE
C          WRITE(6,2040)           JOBFIN,SAMPLE
C          2040 FORMAT(14HOTHERE WILL BE,I3,16H SAMPLES EACH OF,F8.0,10H NEUTRONS.
C          2)
C          IF(ITMAG=1)2043,2042,2043
C          2042 WRITE(6,2041)
C          2041 FORMAT(1H ,31H AUTOMATIC ITERATION REQUESTED.,10X,17H ONE SAMPLE 0
C          1NLY.)
C          JOBFIN=1
C          2043 READ(5,202)STRTE
C          IF(STRTE)205,206,205
C          205 WRITE(6,207)           STRTE
C          207 FORMAT(21H0STARTING ENERGY IS =,F8.3,4H MEV)
C          GO TO 208
C          208 WRITE(6,209)
C          209 FORMAT(41H0STARTING ENERGY IS FROM FISSION SPECTRUM.)
C          208 READ(5,202)           DIST
C          THETAM= COS(ATAN(FRAD/(-DIST-HITE)))
C          WRITE(6,210)THETAM,DIST
C          210 FORMAT(71HUCOSINE OF SEMI-VERTICAL ANGLE OF THE CONE JUST ENCLOSIN
C          26 THE SAMPLE =,F8.6,12H FROM SOURCE,F6.2,22H CMS ALONG THE X AXISNBS0249
C          3.)

```

```

0251
0252
0253
0254
0255
0256
0257
0258
0259
0260
NBS0261
0262
0263
0264
0265
0266
0267
0268
0269
0270
0271
0272
0273
0274
0275
0276
0277
0278
0279
0280
0281
0282
0283
0284
0285
0286
CALL
37
CONTINUE
211
CONTINUE
DO 212 I=1,NSTDOP
IF(THEtam-ANGS(I))212,213,213
CONTINUE
212
CONTINUE
WRITE(6,212)
FORMAT(41HINSUFFICIENT START DISTRIBUTION PROVIDED.)
CALL EXIT
AREA(1)=0.0
STDIST(I)=STDIST(I-1)-(STDIST(I-1)-STDIST(I))*(ANGS(I-1)-ANGS(I))
2ANGS(I-1)-ANGS(I)
ANGS(I)=THEtam
L=I-1
LI=I-1
DO 214 K=1,L
AREA(K+1)=AREA(K)+((STDIST(K+1)+STDIST(K))/2.0)*(ANGS(K)-ANGS(K+1))
2)
214
CONTINUE
DO 215 K=1,64
AIEK
SEG=(AREA(I)*(2.0*AI-1.0))/128.0
DO 216 L=1,I
IF(CAREAL-SEG)216,217,218
CONTINUE
216
FORMAT(63HERROR IN INPUT. PARTIAL SUM LRSS THAN THE TOTAL. CALL
2160

```

```

2EXIT.
)
CALL EXIT
CNPHI(K)=ANGS(L)
GO TO 215
217 GRAD=(STDIST(L)-STDIST(L-1))/(ANGS(L)-ANGS(L-1))
IF(GRAD)300,301,300
300 CNPHI(K)=ANGS(L-1)-(STDIST(L-1)-SQRT(((STDIST(L-1)*STDIST(L-1))-2.*NBS0293
20*GRAD)*(SEG-AREA(L-1)))/GRAD
GO TO 215
218 CNPHI(K)=ANGS(L)+(AREA(L)-SEG)/STDIST(L)
CONINUE
215 WRITE(6,219)(CNPHI(I),I=1,64)
219 FORMAT(5H004 EQUITY-PROBABLE COSINES OF THE START DISTRIBUTION ARE/
2(8F14.6))
TANGLE=AN(ANGLE)
RINC=WHITE*TANGLE**2.
BRADE=FRAD+RINC
FLUXFT=WHITE*(FRAD)**2+FRAD*RINC+(RINC**2)/3)/((DIST+HITE)**2)*
1(1-THETAM)
M1=IXMAT+2*NMATS
FNEGSENEG$-1.0
NMAT+4*NMATS
MISSM=IUMAT(N)
UINELOG (STRTE/6.25E-7)
SESTRTE
LGR=1
IF(S-EMC(1))5000,5000,4999
4999 IF(NEGS-128)4001,4001,5001
5001 NM=129
LGREM
IF(S-EMC(M))5002,5000,5003
5002 MEM=64
GO TO 4020
5003 MEM+64
GO TO 4020
4001 M=65

```

```

4020 LGR=M
  IF(S-EMC(M))4030,50000,4040
4030 M=M-32
  GO TO 4050
4040 M=M+32
4050 LGR=M
  IF(S-EMC(M))4060,50000,4070
4060 N=M-16(1)
  GO TO 4080
4070 M=M+16
4080 LGR=M
  IF(S-EMC(M))4090,50000,4100
4090 M=M-8
  GO TO 4110
4100 M=M+8
4110 LGR=M
  IF(S-EMC(M))4120,50000,4130
4120 M=M-4
  GO TO 4140
4130 M=M+4
4140 LGR=M
  IF(S-EMC(M))4150,50000,4160
4150 M=M-2
  GO TO 4170
4160 M=M+2
4170 LGR=M
  IF(S-EMC(M))4180,50000,4190
4180 M=M-1
  GO TO 4200
4190 M=M+1
4200 LGR=M
  IF(S-EMC(M))4210,50000,5000
5000 M2=1DATA(M1)+LGR-MISSM
AVPATH=DATA(N2)
FLUXFT=FLUXFT/AVPATH

```

0313
0314

```

AVCOS=(CNPH1(32)+CNPH1(33))/2.0
DO 2150 I=1,LI
IF (ANGS (I+1)-AVCOS)2151,2152,2150
CONTINUE
I=LI
2151 FACT=STDIST(I)-(STDIST(I+1))*(ANGS (I)-AVCOS)/(ANGS (I)
2-ANGS (I+1))
GO TO 2153
2152 FACT=STDIST(I)
FLUXFT=FLUXFT*STDIST(I)/FACT
READ(5,201)NLWREV
READ(5,220)(LAWREV(I),I=1,NLWREV)
WRITE(6,2193)
FORMAT(38HOLAW REFERENCE NUMBER M.C.LAW NUMBER.)
WRITE(6,2194)(LAWREV(I),I=1,NLWREV)
2193 FORMAT(10,10X,I10)
IF(LFB4)2192,234,2192
2192 READ(5,201)IANALA,IANALB,IANALC,IANALD
READ(5,220)
READ(5,220)
FORMAT(2110)
FORMAT(2110)
WRITE(6,221)ANAL
FORMAT(15H054 ANALYSIS ON,I3,10H ACTIONS.)
WRITE(6,222)
(NUCL(I),I=1,NANAL)
222 FORMAT(15HNUCLIDE NOS. '24I4)
WRITE(6,223)
(NAC1(I),I=1,NANAL)
223 FORMAT(16HOK.P.ACTION NOS.,I3,23I4)
M3=N1-NMATS
IXNUC1=IDATA(M3)
M4=M3+4*NMATS
NUCS=IDATA(M4)
DO 3 I=1,NANAL
M5=IXNUC1+NUCL(I)
M6=8*NUCS+M5
NOACA(I)=IDATA(M6)
IXACT1(I)=IDATA(M5)
0315
0316
0317
0318
0319
0320
0321
0322
0323
0324
0325
0326
0327
0328
0329
0330
0331
0332
0333
0334
0335
0336
0337
0338
0339
0340
0341
0342
0343
0344
NBS0345
0346
0347
0348
0349
0350
0351
0352
0353
0354
0355
0356
0357
0358

```

```

0359
K=1          0360
NOACA1=NOACA(1) 0361
DO 4 J=1,NOACA1 0362
L=MMMK+K      0363
IF (IDATA(L)=NAC1(I))7,5,7 0364
K=K+1          0365
CONTINUE       0366
        WRITE(6,6)      NAC1(I)
        CALL EXIT
NACT(I)=K      0367
CONTINUE       0368
FORMAT(18H K.P.ACTION NUMBER,I4,29H DOES NOT APPEAR IN THE DATA.) 0369
FORMAT(15HUM.C.ACTION NO.,24I4) 0370
FORMAT(15HUM.C.ACTION NO.,24I4) 0371
FORMAT(15HUM.C.ACTION NO.,24I4) 0372
FORMAT(15HUM.C.ACTION NO.,24I4) 0373
FORMAT(15HUM.C.ACTION NO.,24I4) 0374
READ(5,202) FCCOS(I),I=1,33) 0375
C   33 COSINES WITH 33 VALUES OF THE ANGULAR DISTRIBUTION MUST BE 0375
C   SUPPLIED, WITH MONOTONICALLY INCREASING VALUES OF THE COSINE. 0376
DO 225 JE1,NANAL 0377
READ(5,202)(FCVAL(J,I),I=1,33) 0378
AREB=0.0         0379
DO 228 I=1,32
AREB=AREB+ABS (FCCOS(I+1)-FCCOS(I))*(FCVAL(J,I)+FCVAL(J,I+1))/2.0NBS0381 0380
2)
CONTINUE       0382
IA=1           0383
IB=15          0384
FORMAT(6,226)(FCCOS(I),I=IA,IB) 0385
FORMAT(15HCOSINES ,15F7.3) 0386
FORMAT(15H COSINES ,15F7.3) 0387
FORMAT(6,227)(FCVAL(J,I),I=IA,IB) 0388
FORMAT(15H DISTRIBUTION ,15F7.3) 0389
DO 229 I=IA,IB 0390
FCVAL(J,I)=FCVAL(J,I)/AREB 0391
CONTINUE       0392
FORMAT(6,230)(FCVAL(J,I),I=IA,IB) 0393
FORMAT(15H UIFF,X SECT.,15F7.3) 0394

```

```

IF(IA-1)2300,2300,2301
2300 IA=16          0395
      IB=30          0396
      GO TO 2<80     0397
2301 IF(IA-16)2302,2302,225 0398
2302 IA=31          0400
      IB=33          0401
      GO TO 2280     0402
225  CONTINUE       0403
      IMINM=1         0404
      DO 252 L=1,NANAL
      IMIN(L)=IMINM
      READ(5,250)IMAX(L)
250  FORMAT(1I10)
      PRINT 251,IMAX(L),L
251  FORMAT(1UHUTHERE ARE,I2,4H SUPPLEMENTARY RANGES ASSOCIATED WITH ANBS0410
2NALYSIS,I2)
      IF(IMAX(L)>252,252,253
      IMAXM=IMAX(L)-1+IMINM
      DO 254 I=IMINM,IMAXM
      READ(5,202)ENVAL(L,I)
      READ(5,202)(SUPVAL(I,K),K=1,33)
      AREB=0.0
      DO 258 J=1,32
      AREB=AREB+ABS (FCCOS(J+1)-FCCOS(J))*((SUPVAL(I,J)+SUPVAL(I,J+1))/2NBS0419
      2.0)
258  CONTINUE       0418
      IA=1           0420
      IB=15          0421
      WRITE(6,258J)ENVAL(L,I)
2580 FORMAT(25H0 THIS RANGE APPLIES BELOW,F7.4,5H MEV.)
      WRITE(6,226)(FCOS(J),J=IA,IB)
      WRITE(6,227)(SUPVAL(I,J),J=IA,IB)
      DO 260 J=IA,IB
      SUPVAL(I,J)=SUPVAL(I,J)/AREB
      CONTINUE       0423
0424
0425
0426
0427
0428
0429
0430

```

```

      WRITE(6,230)(SUPVAL(I,J),J=IA,IB)          0431
      1F((IA-1)261,261,262                      0432
261    IA=16                                     0433
         IB=30                                     0434
         GO TO 259                                 0435
262    IF((IA-16)263,263,254                     0436
263    IA=31                                     0437
         IB=33                                     0438
         GO TO 259                                 0439
254    CONTINUE                                   0440
         IMIN=IMAX+1                             NBS0441
         IF((IMAX-24)252,252,256                 0442
         WRITE(6,257)                               0443
         FORMAT(27H1IMAX HAS EXCEEDED 24-HALT.)  0444
         CALL EXIT                                  0445
252    CONTINUE                                   0446
         READ(5,201)NOCOU                         0447
         READ(5,202)                               (COUNT(I),I=1,NOCOU)
         WRITE(6,232)                               NOCOU,(COUNT(I),I=1,NOCOU)
232    FORMAT(10H0THERE ARE,I3,56H COUNTERS LOCATED AROUND THE EQUATOR OFNBS0450
         2 THE SCATTERER AT/(10F9.4)               NBS0451
         READ(5,201)                               NENSP
         READ(5,202)                               (ENSP(I),I=1,NENSP)
         WRITE(6,233)                               (ENSP(I),I=1,NENSP)
233    FORMAT(48H0THE ENERGY SPECTRA OF THE B4 ANALYSIS CELLS ARE/(10F9.3
         2))                                0455
234    DO 2340 K=1,32                           0456
         FCCOSD(K)=FCCOS(K+1)-FCCOS(K)
2340  CONTINUE                                   0457
         RETURN                                     0458
END                                         0459
                                         0460
                                         0463

```

C TRUNCATED CONE SCATTERING SAMPLE, INCIDENT NEUTRONS ALONG THE AXISNBS

```

INCLUDE CINC1
DIMENSION TEMP(10),TRIG(4)
61  TEMPENRANDA(64)
WORK3=CECnPHI(ITEMP)
62  TEMP(1)=ERANDA(-1)
TEMP(2)=ERANDA(-2)
TEMP(3)=TEMP(1)*TEMP(1)
TEMP(4)=TEMP(2)*TEMP(2)
TEMP(5)=TEMP(3)+TEMP(4)
IF(TEMP(5)>6.2)62,62,63
IF(TEMP(5)-1.0>6.2)62,62,63
63  TRIG(1)=(TEMP(3)-TEMP(4))/TEMP(5)
TRIG(2)=(2.0*TEMP(1)*TEMP(2))/TEMP(5)
TRIG(3)=SQRT((1.0-WORK3*WORK3))
WORK4=TRIG(1)*TRIG(3)
WORK5=TRIG(2)*TRIG(3)
C DOES THE NEUTRON HIT THE TARGET
C
TEMP(1)=FRAU+(DIST+HITE)*TRIG(3)/WORK3
IF(TEMP(1)>6.7)67,67,65
65  TEMP(2)=(DIST+HITE)/WORK3
TEMP6=-HITE
66  WORK7=WORK4*TEMP(2)
WORK8=WORK5*TEMP(2)
ANEUNO=ANEUNO+1.0
EINSTRTE
UIN=LOG(EIN/0.25E-7)
MAT=1
IWORK1=0
WORK19=0.0
WIN=1.0
NBS3121 3116
NBS3121 3122
EU. 3124
EU. 3126
NBS3127 3127
NBS3128 3128
NBS3129 3129
NBS3130 3130
NBS3131 3131
NBS3132 3132
NBS3133 3133
NBS3134 3134
NBS3135 3135
NBS3136 3136
NBS3137 3137
NBS3138 3138
NBS3139 3139
NBS3140 3140
NBS3142 3142
NBS3143 3143
NBS3145 3145
NBS3146 3146
NBS3147 3147
NBS3148 3148
NBS3149 3149
NBS3150 3150
NBS3151 3151
3152
3153
3154

```

WORK11=0•0
IWORK2=0
RETURN
AMISS=AMISS+1•0
GO TO 61
END

67

3155
3156
3157
3158
3159
3160

SUBROUTINE TRACK

C TRACKS NEUTRONS IN A TRUNCATED CONE WITH AXIS LYING ALONG THE NEUTRON BEAM

```

INCLUDE CINC1
CALL E6MV
PATHL=(-(LOG(RANDA(1)))*PATH
IF (WORK3)1,6,2
1 TRS=-(HITE+WORK6)/WORK3
RAD2=FRAD**2
GO TO 3
2 TRS=(HITE-WORK6)/WORK3
RAD2=BRAD**2
3 WORK17=WORK7+TRS*WORK4
WORK18=WORK8+TRS*WORK5
TRR2=WORK17**2+WORK18**2
IF (RAD2.LT.TRR2) GO TO 6
IF (TRS.GT.PATHL) GO TO 13
ISCOLL=2
IF (WORK3.GT.0) GO TO 4
WORK16=-HITE
GO TO 5
4 WORK16=HITE
5 WORK19=WORK19+TRS/SPEED
RETURN
6 CALL FONEC(PATHL)
IF (HITE.LE.ABS(WORK16)) GO TO 7
TRA2=WORK17**2+WORK18**2
RAD2=(FRAD+(HITE+WORK16)*TANGLE)**2
IF (RAD2.GT.TRA2) GO TO 14
7 ISCOLL=1
NRTS=0
RAD=FRAD+(HITE+WORK6)*TANGLE
TA=1.-WORK3**2*(1.+TANGLE**2)
TB=WORK7*WORK4+WORK8*WORK5-WORK3*TANGLE*RAD

```

```

TC=WORK7**2+WORK8**2-RAD**2
IF(ABS(TA).GT.1.E-30)GO TO 8
IF(ABS(TB).LT.1.E-30)GO TO 21
TR=-TC/(2.*TB)
GO TO 12
8 TD=TB*TB-TA*TC
   IF(TD)15,10,9
9 TE=-TB+SQRT(TD)
   IF(TE.LT.0)GO TO 10
NRTS=1
TR=TE/TA
10 TE=-TB-SQRT(TD)
   IF(TE.LT.0)GO TO 11
NRTS=NRTS+1
TR=TE/TA
11 IF(NRTS-1)17,12,19
12 CALL FONEC(TR)
WORK19=WORK19+TR/SPEED
RETURN

13 CALL FONEC(PATHL)
14 ISCOLL=3
WORK19=WORK19+PATHL/SPEED
RETURN

C      ERROR EXITS

15 WRITE(6,16)
16 FORMAT(24H IMAGINARY ROOT IN TRACK)
   GO TO 23
17 WRITE(6,18)
18 FORMAT(26H NO POSITIVE ROOT IN TRACK)
   GO TO 23
19 WRITE(6,20)
20 FORMAT(28H TWO POSITIVE ROOTS IN TRACK)
   GO TO 23

```

```
21 WRITE(6,22)
22 FORMAT(22H INDETERMINATE ROOT IN TRACK)
23 WRITE(6,24) WORK3,WORK4,WORK5,WORK6,WORK7,WORK8,PATHL
24 FORMAT(7F10.3)
      CALL EXIT
      END
```

```

INCLUDE CINC1
DIMENSION FACT(33), PATHLL(33), ANGLEE(33), KL(33)
NENSP1=NENSP-1
M1=IXMAT+NMAT+NMAT
NEM1+4*NMATS
MISSM=IDATA(1)
K2=IDATA(M1)-MISSM
DO 1 I=1, NOCOU
COSOMECOUNT(I)
CALL FPATH(COSOM, PATHL, ANGLEF)
DO 2 K=1, 32
IF(FCCOS(K+1)-ANGLEF)2,3,3
CONTINUE
2
K=32
AFCOS=FCCOS(K)
FACT(I)=(ANGLEF-AFCOS)/FCCOSD(K)
PATHLL(I)=PATHL
ANGLEE(I)=ANGLEF
KL(I)=K
CONTINUE
DO 7 J=1, NATOM
NFORM=0
NAC=NAC1(J)
NUCLID=NUCL(J)
PART=PART1(J)
ATOM=ATOM1(J)
WSQ=ATOM*ATOM-1.0
DO 8 I=1, NOCOU
KEKL(I)
AS=ANGLEE(I)
FACTOR=FACT(I)
PATHL=PATHLL(I)
ASQ=AS*AS
IF(PART)7,7,8
3

```

```

8      IF (NAC-2) 9,10,9
10     X=SQRT (ASQ+NSQ)
11     P=((AS+X)/(ATOM+1.0))*( (AS+X)/(ATOM+1.0))
12     REDEN=EN*P
13     GO TO 11
14     IF (INFORM) 34,34,35
15     CALL CRDN
16     REDEN=EN*ER
17     IF (REDEN) 38,11,11
18     60 TO (36,11,11,11,11,11,36,11,11,11,11,11,11,11)
19     P=(AS+SQRT (ASQ+ATOM*QV*(1.0+ATOM)/EIN+NSQ))/(1.0+ATOM)
20     REDEN=EN*I*P
21     11 IF (IMAX(J).LE.0) GO TO 15
22     IMINM=IMIN(J)
23     IMAXM=IMINM+IMAX(J)-1
24     DO 50 JJ=IMINM,IMAXM
25     IF (EIN-ENVAL(J,JJ)) 50,51,52
26     CONTINUE
27     51 KK=JJ
28     GO TO 19
29     52 IF (JJ.LL.IMINM) GO TO 15
30     KK=JJ-1
31     GO TO 19
32     15 SIGMA=(FCVAL(J,K+1)-FCVAL(J,K))*FACTOR+FCVAL(J,K)
33     60 TO 16
34     19 SIGMA=(SUPVAL(KK,K+1)-SUPVAL(KK,K))*FACTOR+SUPVAL(KK,K)
35     16 DO 20 L=1,NENSP1
36     20 IF (ENSP(L+1)-REDEN) 20,21,21
37     CONTINUE
38     L=NENSP1
39     SEREDEN
40     LGRE=M
41
42     IF (S-EMC(1)) 5000,5000,4999
43     IF (NEGS-128) 4001,4001,5001
44     M=129
45     LGR=M
46
47     EU.
48     NBS EU.
49     EU.
50     EU.
51     EU.NBS

```

```

EU.   IF(S=EMC(M))5002,5000,5003
5002 M=M-64
      GO TO 4020
      M=M+64
      GO TO 4020
      M=65
      LGR=M
      IF(S=EMC(M))4030,5000,4040
      M=M-32
      GO TO 4050
      M=M+32
      LGR=M
      IF(S=EMC(M))4060,5000,4070
      M=M-16
      GO TO 4080
      M=M+16
      LGR=M
      IF(S=EMC(M))4090,5000,4100
      M=M-8
      GO TO 4110
      N=M+8
      LGR=M
      IF(S=EMC(M))4120,5000,4130
      M=M-4
      GO TO 4140
      M=M+4
      LGR=M
      IF(S=EMC(M))4150,5000,4160
      M=M-2
      GO TO 4170
      M=M+2
      LGR=M
      IF(S=EMC(M))4180,5000,4190
      M=M-1
      GO TO 4260
      M=M+1

```

```

4200 LGR=M
    IF(S-EMC(M))4210,5000,5000
4210 LGR=N-1
5000 M3=M2+LGR
    PATHB=(-DATA(M3))
    QU=J(J)
    PTH=PATHL/PATHB
    ADD=QU*SIGMA*EXP(PTH)
    DEA(I,L)=DEA(I,L)+ADD
    IF(NAC.NE.2)GO TO 24
    IF(IWORK1.LE.1)GO TO 23
    III=IWORK1-1
DO 22 II=1,III
    IF(ICOLL(II).NE.1)GO TO 24
    CONTINUE
22  DEB(I,L)=DEB(I,L)+ADD
    IF(IWORK1.LE.1)GO TO 0
    DED(I,L)=DED(I,L)+ADD
    GO TO 6
24  DEC(I,L)=DEC(I,L)+ADD
    CONTINUE
6   GO TO 40
7   CONTINUE
38  PRINT 39,REDEN
39  FORMAT(1H0,F10.4,32HNEGATIVE ENERGY COMPUTED IN CREN)
    CALL EXIT
40  RETURN
END

```

```

SUBROUTINE FPATH(COSOM,PATHL,ANGLEF)
C      PATH LENGTH AND ANGLE FOR B4 ANALYSIS. FOR TRUNCATED CONE SAMPLE.
C      AXIS ALONG THE INCIDENT NEUTRON BEAM.

INCLUDE CINC1

C      NEUTRON OUT AT 90 DEGREES.
IF(ABS(COSOM).GE.1.E-5)GO TO 1
ANGLEF=WORK4
TSQ=TANGLE**2
XPR=FRAU/TANGLE+HITE+WORK16
PATHL=SQRT(XPR*XPR*TSQ-WORK18**2)-WORK17
RETURN

C      NEUTRON OUT ENTRANCE FACE
1  SINOMESQRT(1.-COSOM**2)
ANGLEF=COSOM*WORK3+SINOM*WORK4
IF(COSOM.GT.0)GO TO 2
IF(FRAD.LT.ABS(WORK18))GO TO 3
FTAN=(SQRT(FRAD**2-WORK18**2)-WORK17)/(HITE+WORK16)
TANOM=SINOM/COSOM
IF(FTAN+TANOM.LT.0)GO TO 3
PATHL=-(HITE+WORK16)/COSOM
RETURN

C      NEUTRON OUT EXIT FACE
2  BTAN=(SQRT(BRAD**2-WORK18**2)-WORK17)/(HITE-WORK16)
TANOM=SINOM/COSOM
IF(BTAN.LT.TANOM)GO TO 3
PATHL=(HITE+WORK16)/COSOM
RETURN

C      NEUTRON OUT THE SIDE, BUT NOT AT 90 DEGREES, NORMAL SOLUTION.
3  TSQ=TANGLE**2
XPR=FRAU/TANGLE+HITE+WORK16

```

```
PA=SINOM**2-(COSOM**2)*TSQ
PB=WORK17*SINOM-XPR*COSOM*TSQ
PC=WORK17**2-(XPR**2)*TSQ+WORK18**2
IF (ABS(PA).LT.1.E-30) GO TO 4
PATHL=(SQR1(PB**2-PA*PC)-PB)/PA
RETURN
```

```
C   LINEAR SOLUTION
4 PATHL=-PC/(2.*P13)
RETURN
END
```

```

C          SUBROUTINE FPATH(COSOM,PATHL,ANGLEF)
C          PATH LENGTH AND ANGLE FOR THE B4 ANALYSIS, FOR A CYLINDRICAL SAMPLE
C          WITH ITS AXIS ALONG THE INCIDENT NEUTRON BEAM.

INCLUDE CINC1
PATHL=SQRT(FRAD**2-WORK18**2)-WORK17
IF(ABS(COSOM).GT.1E-5)GO TO 1
ANGLEF=WORK4
GO TO 3
1 SINOM=SQRT(1-COSOM**2)
TANOM=SINOM/COSOM
ANGLEF=COSOM*WORK3+SINOM*WORK4
IF(COSOM.GT.1E-5)GO TO 2
FTAN=PATHL/(HITE+WORK16)
IF((FTAN+TANOM).LT.1E-5)GO TO 3
PATHL=(HITE+WORK16)/COSOM
RETURN
2 FTAN=PATHL/(HITE-WORK16)
IF(FTAN.LT.TANOM)GO TO 3
PATHL=(HITE+WORK16)/COSOM
RETURN
3 PATHL=PATHL/SINOM
RETURN
END

```

C SUBROUTINE OUTPUTS RESULTS AT THE END OF EACH SAMPLE.

```

INCLUDE CINC1
DIMENSION P(33)
PRINT 1, (HEAD(I), I=1,12)
1 FORMAT(12A6)          2, NO SAMP
2 PRINT 1H0,52X,13HSAMPLE NUMBER,I3)      3, SAMPLE
3 PRINT 1H0,40X,F8.0,33H NEUTRONS STARTED IN EACH SAMPLE.)
4 PART = NO SAMP
TOT = PART * SAMPLE
PRINT 5, TOT
5 FORMAT(1H0,39X,F9.0,35H NEUTRONS HAVE BEEN TRACKED SO FAR.)
PRINT 4, PESC,CESC
6 FORMAT(24HUPLANE SURFACE ESCAPES =,F11.3/24H0CURVED SURFACE ESCAPE
25,F11.3)
7 CALL OUTB3
8 IF(IENNSP-1)
9 IF(IFB4.EG.0)GO TO 7
10 CALL OUTB4(DEA,1,IANALA)
11 IF(IANALA.LE.0)GO TO 8
DO 6 I=1,II
12 P(I)=DEA(IANALA,I)
13 CALL APLOT3(P,I1,ENSP,IANALA)
14 CALL OUTB4(DEB,2,IANALB)
15 IF(IANALB.LE.0)GO TO 10
DO 9 I=1,II
16 P(I)=DEB(IANALB,I)
17 CALL APLOT3(P,I1,ENSP,IANALB)
18 CALL OUTB4(DEC,3,IANALC)
19 IF(IANALC.LE.0)GO TO 12
DO 11 I=1,II
20 P(I)=DEC(IANALC,I)
21 CALL APLOT3(P,I1,ENSP,IANALC)
NBS 3958
NBS 3960
NBS 3961
NBS 3962
NBS 3963
NBS 3964
NBS 3965
NBS 3966
NBS 3967
NBS 3968
NBS 3969
NBS 3970
NBS 3971
NBS 3972
NBS 3973
NBS 3974
NBS 3975
NBS 3976
NBS 3977
NBS 3978
NBS 3979
NBS 3980
NBS 3981
NBS 3982
NBS 3984
NBS 3985
NBS 3986
NBS 3987
NBS 3988
NBS 3991
NBS 3992
NBS 3993
NBS 3994
NBS 3996

```

```
12 CALL OUT34(JED,4,IANALD)
   IF(IANALD.LE.0) GO TO 7
   DO 13 I=1,I1
      P(I)=JED(IANALD,I)
      CALL APLOT3(P,I1,ENSP,IANALD)
   13 RETURN
   END
```

12

13

7

```
CALL OUT34(JED,4,IANALD)
IF(IANALD.LE.0) GO TO 7
DO 13 I=1,I1
P(I)=JED(IANALD,I)
CALL APLOT3(P,I1,ENSP,IANALD)
```

```
NBS3998
NBS3999
NBS4000
NBS4001
4003
4004
4005
```

SUBROUTINE AUTO

C TO ALLOW AUTOMATIC ITERATION UNDER THE FOLLOWING CONDITIONS.
 C NUMBER OF COUNTERS AND INPUT POINTS = 33.
 C ONE NUCLIDE ONLY.
 C ELASTIC CORRECTION ONLY.
 C PHYSICAL ITERATION.
 C $(\Delta \Sigma)/(\Sigma)$ IS THE CHANGE IN THE CROSS SECTION EXCLUDING
 C MULTIPLE SCATTERING.

```

INCLUDE CINCL
DIMENSION TOTEL(33),CHI(33),ELM2(33),XIP3(33)
SUMEL=(DEB(1,33)+DEB(33,33))/32.0
DO 4 J=2,32
SUMEL=SUMEL+IEE(J,33)/16.0
4 CONTINUE
IF (ITER.NE.1) GO TO 300
READ(5,101)INTERM,IFCONT
101 FORMAT(2I10)
INTERM=INTERM-1
IF(IFCONT.EQ.0)GO TO 100
READ(5,104)(EZP(I),I=1,33)
104 FORMAT(6F10.4)
SUMEZP=(EZP(1)+EZP(33))/32
DO 107 J=2,32
SUMEZP=SUMELZP+EZP(J)/16
DO 108 J=1,33
108 EZP(J)=EZP(J)/SUMEZP
GO TO 102
100 DO 105 I=1,33
EZP(I)=FCVAL(1,I)
105 CONTINUL
102 IF(INTERM.LE.1)GO TO 300
106 READ(5,103)(SAMP(I),I=1,INTERM)
103 FORMAT(6F10.2)
300 CHISQ=0.0
      1977
      1978
      1979
      1980
      1981
      NBS
      NBS2062
      2065
      2066
      2067
      2068
      NBS2073
      NBS2077
      NBS2078
      2079
      NBS
      NBS
      NBS
      NBS
      NBS
      NBS
      NBS
      NBS
      NBS
      2074
      NBS2075
      2076
      NBS2080
      NBS2081
      2082
      2086

```

```

DO 303 J=1,33          NBS2087
TOTEL(J)=DEB(J,33)/SUMEL   2088
CHI(J)=(TOTEL(J)-EZP(J))*2/EZP(J)  NBS2089
CHISQECHI=CHI(J)           2090
DEDNJ=DED(J,33)/SUMEL     NBS
ELM2(J)=FCVAL(1,J)        2097
FACTOR=(TOTEL(J)-DEDNJ)/ELM2(J)
IF(ITER.GT.2) GO TO 302   NBS
XIP3(J)=(EZP(J)-DENJ)/FACTOR
GO TO 303                 NBS
302 XIP3(J)=FCVAL(1,J)/FACTOR
303 CONTINUE                NBS
214 SUM=(XIP3(1)+XIP3(33))/32.0  2098
DO 207 J=2,32              2099
SUM=SUM+XIP3(J)/16.0       2100
207 CONTINUE                2101
DO 208 I=1,33              2102
FCVAL(I,1)=(XIP3(I))/SUM  2103
208 CONTINUE                2104
DO 220 I=1,33              2105
XIP3(I)=DEB(I,33)-DED(I,33)
SUMSEL=(XIP3(1)+XIP(33))/32
DO 221 I=2,32
SUMSEL=SUMSEL+XIP3(I)/16
DO 222 I=1,33
XIP3(I)=(XIP3(I)/SUMSEL-ELM2(I))/ELM2(I)
222 PRINT 209,ITER          NBS
209 FORMAT(1H1,20H AFTER ITERATION NO.,13,49H * NORMALISATION IS UNIT
1AREA FOR ELASTIC EVENTS.)  2106
216 ITER1=ITER+1            2107
PRINT 210,ITER,ITER,ITER,ITER  2108
210 FORMAT(1H0,7HCOUNTER,4X,6HCOSINE,11X,3HEXP,7X,10HOUTPUT NO.,12,4X,
13HNO.,12,5H CHI ,7X,3HNO.,12,11X,3HNO.,12,4X,11HDELTA SIGMA,2X, 2111
27HCOUNTER/2X,6HNUMBER,5X,5HANGLE,10X,5HINPUT,7X,11HALL ELASTIC,6X,  NBS2112
37HSQUARED,8X,5HINPUT,11X,5HINPUT,9X,6H/SIGMA,2X,6HNUMBER)  2113
PRINT 111,(J,COUNT(J),EZP(J),TOTEL(J),CHI(J),ELM2(J),FCVAL(1,J),  NBS2114
NBS2115

```

NBS2116
2117
2118
2119
2120
2121
2122
2123
2124
2125
2126
2127
2128
2129
2130

```
1XIP3(J),J=1,33)
111 FORMAT(14,7F15.6,I4)
112 PRINT 112,CHISQ
112 FORMAT(1H0,3HCHISQ = 'F10.6)
997 IF (ITER-INTERM)415,416,416
415 SAMPLE=SAMP(ITER)
        ITER=ITER+1
        GO TO 999
416 ITER=10
        GO TO 998
999 CALL DATIN
998 RETURN
      END
```

SUBROUTINE RANDOM(ISTART)

```

DATA MASK/03777777777777/
MULTA/30517578125/,C/.29103830E-10/
IRSTART
RETURN
ENTRY RDM(R)
IRE=AND(MASK,IR*MULTA)
K=C*(FLCAT(IR))
RETURN
END

```

FUNCTION RANDA(I)

```

CALL RDM(R)
RANDA=R
IF(I)1,1,3
1 RANDA=RANDA*2.-1.
3 RETURN
END

```

EU•4009

```

NBS4010
NBS4010A
EU•4011
EU•4012
EU•4013
EU•4014

```

FUNCTION NRANDA(I)

```

CALL RDM(XRAND)
IF(XRAND)10,10,1
1 IF(XRAND-1.)20,30,30
10 NRANDA=1
GO TO 40
20 NRANDA=XRAND*1+1
GO TO 40
30 NRANDA=1
40 RETURN
END

```

EU•0002

```

NBS0003
EU•0004
EU•0005
EU•0006
EU•0007
EU•0008
EU•0009
EU•0010
EU•0011
EU•0012

```

A Brief Description of the Components of MAGGIE

1. MAGGIE (Main Program). This program calls the various subroutines required for the analysis, retrieves neutrons from disc storage when required, outputs track parameters if desired, and records the various fates of tracked neutrons.
2. RANDOM (and RDM). This subroutine contains the random number generator, RDM, as a separate entry. RANDOM is called at the beginning of program MAGGIE to enter the starting value for RDM.
3. DATIN serves to set all of the output arrays to zero, and calls ABSYND.
4. ABSYND reads the required nuclear data from the MOULD tape and puts it in encoded sequential storage in the array DATA-IDATA for use during the Monte Carlo tracking.
5. INPUT reads and processes samples and experimental angular distribution data from card input and calculates most of the flux attenuation factor.
6. CRNEU creates random incident neutrons at the entrance face of the sample, in accordance with the input source distribution.
7. TRACK tracks neutrons in the sample, specifying coordinates of collision or escape.
8. EGMV. This subroutine computes the mean free path, velocity, and lethargy group number.
9. FONEC calculates coordinates at the end of a track from initial position, direction cosines, and track length.
10. CR. This subroutine, using random sampling of the information stored by ABSYND from the MOULD data tape, determines all of the parameters of a collision.
11. CALC determines some constants used in subroutine NAPAN.
12. NAPAN. This subroutine calculates and scores the probability of detection at each detector for each collision in the sample.
13. FPATH calculates the path length in the direction of each detector for each collision.
14. CREN is an abbreviated version of CR used by NAPAN that determines only the neutron energy.

15. TWIST chooses new direction cosines after a collision.
16. WRTBT stores any secondary neutrons produced, for recall at the end of the current tracking.
17. OUTPUT, OUTB3, OUTB4 and APLOT3. These subroutines print the results of the calculation.
18. AUTO performs the calculations required for iterative correction of the elastic angular distribution, prints the current output, and calls DATIN to begin the next iteration.
19. END, and its entries EXIT and EEXIT designate normal vs. error exit conditions.
20. TAPLAB returns the tape logical unit label.
21. SRFORT is a subroutine for skipping tape records.

APPENDIX C

Input requirements for MAGGIE-NBS

<u>FORMAT</u>	<u>VARIABLE</u>	<u>COMMENTS</u>
1. 012	OCT	Octal starting value for RDM.
2. 12A6	HEAD(I)	Arbitrary heading. Column one should be a 1.
3. I10	NMATS	The number of materials in the sample. This is always = 1.
4. I10, E10.4	IDATA(MAT5) DATA(MAT4)	Number of different nuclides in the material. Density of the material.
5. I10, E10.4	IDATA(K2) DATA(K4)	Nuclide reference number (i.e. position on the MOULD tape: see output of MOULD for this). Proportion of this nuclide in the material. This card is repeated for each nuclide in the material.
6. 2I10	IFB4 NSENSE	Positive for B4 output. Positive for track print.
7. 3F10.4	HITE FRAD ANGLE	Length of the samples, in cm. Entrance radius of same, in cm. Half-angle of same, in radians.
8. 2I10	JOBFIN ITMAG	Number of independant samples (= 1 if ITMAG > 0). Positive for automatic iteration.
9. F10.4	SAMPLE	Number of neutrons in each sample.
10. F10.4	STRTE	Starting energy in MeV. If the starting energy is set = 0 a fission spectrum is assumed.
11. F10.4	DIST	Distance from the center of the sample to the source (negative), in cm.
12. I10	NSTD _P	No. of start distribution points to be read in (≤ 25).
13. 6F10.4	ANGS(I)	Three pairs to a card, the angle and start distribution for that angle. The start distribution need not be normalized, and this card is repeated until NSTD _P pairs are read in.

14. I10

NLWREV

The number of Law Reference numbers for inelastic scatter, i.e. the number of Law Reference numbers to different angular distributions on the MOULD output (P.C.N.'s* 4-15 only) (NLWREV \leq 50).

15. 2I10

LAWREV(I)
LWNO(I)

One pair per card, the above Law Reference numbers and the monotonically increasing "Monte Carlo" law numbers allocated. Any inelastic law not given here will be printed in the B3 section results under Law zero.

NOTE: The following cards are not required if IFB4 \leq 0.

16. 4I10

IANALA
IANALB
IANALC
IANALD

Four markers, for the tables: A) Complete multiple scatter analysis. B) Elastic events only. C) Inelastic events only. D) Multiple elastic events only. A negative marker suppresses the table. A positive marker = N produces, in addition to the table, a graph for the Nth counter.

17. I10

NANAL

Number of actions (index I below) (i.e. different neutron processes, such as elastic, inelastic from the 1st excited state, etc.) to be processed by the subroutine NAPAN.

18. 6F10.4

NUCL(I)
NAC1(I)

The nuclide reference number (as in card 5), and the P.C.N.* for each action. There are NANAL such pairs.

19. 6F10.4

FCCOS(J)

Thirty-three values of cosine, including -1 and +1, monotonically increasing.

20. 6F10.4

FCVAL(I,J)

Thirty-three values of the angular distribution (index J) corresponding to the above values of cosines. Repeat for each action (index I) in the same order as in 18.

NOTE: The following three items are repeated, as a group, for each action.

21. I10

IMAX(I)

Number (index L) of supplementary ranges for this action (even if zero).

* The "P.C.N.'s (Particular Classification Numbers) are listed starting on p.8 of AWRE report no. O 70/63, "The Aldermaston Nuclear Data Library as at May, 1963", K. Parker.

NOTE: The following two items are repeated for each supplementary range. If, for any action, there is no supplementary range these items are omitted.

22.	F10.4	ENVAL(I, L)	Upper limit of the range in MeV. These must be listed in order of decreasing value.
23.	6F10.4	SUPVAL(L, J)	Thirty-three values (index J) of the distribution (range L) at the cosine values FCCOS(J).
24.	I10	NOCOU	Number of counters (≤ 33).
25.	6F10.4	COUNT(I)	Cosines of counter locations.
26.	I10	NENSP	Number of output energy points (≤ 33). The output will be classified into the bins formed by these points.
27.	6F10.6	ENSP(I)	Values of output energy points in MeV.
28.	2I10	NTERM IFCONT	Number of iterations (≤ 10). If this is a continuation of a previous run, for further iterations this should be non-zero (see Section II.c.6.f).
29.	6F10.4	SAMP(I)	Number of neutrons for each iteration, <u>except</u> the first.

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